



A Bayesian framework for inferring dynamic intercellular interactions from time-series single-cell data

Cameron Y Park, Shouvik Mani, Nicolas Beltran-Velez, et al.

Genome Res. published online September 5, 2024

Access the most recent version at doi:[10.1101/gr.279126.124](https://doi.org/10.1101/gr.279126.124)

P<P	Published online September 5, 2024 in advance of the print journal.
Accepted Manuscript	Peer-reviewed and accepted for publication but not copyedited or typeset; accepted manuscript is likely to differ from the final, published version.
Open Access	Freely available online through the <i>Genome Research</i> Open Access option.
Creative Commons License	This manuscript is Open Access. This article, published in <i>Genome Research</i> , is available under a Creative Commons License (Attribution-NonCommercial 4.0 International license), as described at http://creativecommons.org/licenses/by-nc/4.0/ .
Email Alerting Service	Receive free email alerts when new articles cite this article - sign up in the box at the top right corner of the article or click here .



To subscribe to *Genome Research* go to:
<https://genome.cshlp.org/subscriptions>

Published by Cold Spring Harbor Laboratory Press

1 A Bayesian framework for inferring dynamic intercellular
2 interactions from time-series single-cell data

3 Cameron Park^{1,2,12}✉ Shouvik Mani^{2,3,12} Nicolas Beltran-Velez³
4 Katie Maurer^{4,5,6} Teddy Huang^{4,9} Shuqiang Li^{4,9} Satyen Gohil⁴
5 Kenneth J. Livak⁴ David A. Knowles^{3,7,8,10} Catherine J. Wu^{4,5,6},
6 Elham Azizi^{1,2,3,11}✉

7 ¹Department of Biomedical Engineering, Columbia University, New York, NY 10027, USA

8 ²Irving Institute for Cancer Dynamics, Columbia University, New York, NY 10027, USA

9 ³Department of Computer Science, Columbia University, New York, NY 10027, USA

10 ⁴Department of Medical Oncology, Dana-Farber Cancer Institute, Boston, MA, USA

11 ⁵Harvard Medical School, Boston, MA, USA

12 ⁶Broad Institute of MIT and Harvard, Cambridge, MA, USA

13 ⁷Data Science Institute, Columbia University, New York, NY

14 ⁸New York Genome Center, New York, NY

15 ⁹Translational Immunogenomics Laboratory, Dana-Farber Cancer Institute, Boston MA
16 USA

17 ¹⁰Department of Systems Biology, Columbia University, New York, NY

18 ¹¹Data Science Institute, Columbia University, New York, NY

19 ¹²These authors contributed equally

20 cyp2111@columbia.edu ; ea2690@columbia.edu

21 Running title: DIISCO resolves dynamic cell-cell interactions

22 Abstract

23 Characterizing cell-cell communication and tracking its variability over time are crucial for under-
24 standing the coordination of biological processes mediating normal development, disease progression,
25 and responses to perturbations such as therapies. Existing tools fail to capture time-dependent in-
26 tercellular interactions and primarily rely on existing databases compiled from limited contexts.
27 We introduce DIISCO, a Bayesian framework designed to characterize the temporal dynamics of
28 cellular interactions using single-cell RNA-sequencing data from multiple time points. Our method
29 utilizes structured Gaussian process regression to unveil time-resolved interactions among diverse
30 cell types according to their co-evolution and incorporates prior knowledge of receptor-ligand com-
31 plexes. We show the interpretability of DIISCO in simulated data and new data collected from
32 T cells co-cultured with lymphoma cells, demonstrating its potential to uncover dynamic cell-cell
33 crosstalk.

34 Introduction

35 Single-cell RNA sequencing (scRNA-seq) which measures gene expression at the resolution of indi-
36 vidual cells is a powerful technology for elucidating heterogeneous cell types and states (Tirosh et al.,
37 2016; Wilk et al., 2020; Azizi et al., 2018). The recent expansion of single-cell datasets profiling
38 biological systems and longitudinal clinical cohorts over multiple time points offers an exciting op-
39 portunity to characterize the temporal dynamics of cell types and their underlying communication.
40 However, there is an unmet need for computational frameworks that can effectively integrate single-
41 cell data across time points while accounting for temporal dependencies. This need is particularly
42 acute in longitudinal clinical data, where the timing of biopsies cannot be planned or controlled and
43 often varies significantly across patients (Bachireddy et al., 2021).

44 Complex systems such as the tumor microenvironment are constantly evolving, particularly with
45 disease progression or therapeutic interventions. Various cancerous and non-cancerous cell types
46 engage in interactions that lead to diverse treatment outcomes. Uncovering crosstalk between tumor
47 and immune cells (Kumar et al., 2018) for example, can unravel immune dysfunction mechanisms.
48 Furthermore, characterizing the dynamic nature of these interactions and their effect is crucial for
49 understanding mechanisms driving response or resistance to therapies and how these mechanisms

50 can be leveraged to develop more effective therapies (Yofe et al., 2020; Sievers et al., 2023; Maurer
51 et al., 2024).

52 Current approaches for predicting cell-cell interactions using scRNA-seq data rely on existing
53 databases of interacting protein complexes, and they predict interactions based on expression levels
54 of known receptor-ligand (R-L) pairs (Efremova et al., 2020; Browaeys et al., 2020; Jin et al., 2021;
55 Li et al., 2023). However, these methods have several limitations. The effects and expression of R-L
56 subunits can vary across different cell types, a context-dependent nuance often overlooked by existing
57 tools. Reliance on databases also limits the discovery of novel interactions and rare understudied
58 cell types. Finally, existing tools only predict static interactions. They are not capable of inferring
59 dynamic time-varying interactions from integration of time-series datasets and do not obtain the
60 strength or sign of interactions, e.g. inhibitory or activating crosstalk.

61 Here, we present DIISCO (Dynamic Intercellular Interactions in Single Cell transcriptOmics),
62 an open-source tool (https://github.com/azizilab/DIISCO_public) for joint inference of cell type
63 dynamics and communication patterns. DIISCO is a Bayesian framework that infers dynamic inter-
64 actions in scRNA-seq data from non-uniformly sampled time points, incorporates prior knowledge
65 on R-L complexes, and quantifies uncertainty in both its predictions and interpretations. Unlike
66 previous methods, DIISCO can be trained on temporal data to learn how interactions change over
67 time between samples. We demonstrate the performance of DIISCO on simulated data as well
68 as newly generated data collected from chimeric antigen receptor (CAR) T cells interacting with
69 lymphoma cells.

70 In brief, the key contributions of our work are: (1) Construction of a probabilistic framework
71 for modeling temporal dynamics of diverse and interacting cell types in complex biological sys-
72 tems, through the integration of scRNA-seq datasets collected across non-uniformly sampled time
73 points; (2) Development of first-in-class computational tool for predicting time-resolved cell-cell in-
74 teractions, along with the strength and sign (activating or inhibitory) of interactions, empowering
75 discoveries of cell communication associated with progression of biological processes or treatments;
76 (3) A novel Bayesian framework for incorporation of prior knowledge on signaling protein complexes
77 with time-series scRNA-seq data to improve identifiability of dynamic cell interactions and quantify
78 uncertainty; (4) Demonstration of performance in simulated and experimental lymphoma-immune
79 interaction data.

80 Results

81 Overview of DIISCO

82 DIISCO captures the temporal dynamics and interactions of cell types using scRNA-seq data from
83 multiple time points. We define cell types or states as clusters of cells with similar gene expression
84 profiles in scRNA-seq data. The time-series single-cell data are first merged to define unique cell
85 types or states through typical clustering approaches ([Wolf et al., 2018](#); [Levine et al., 2015](#)). The
86 pooling of cells helps with improving statistical power in the detection of rare cell types. Then, the
87 number of cells assigned to each cell type at each time point is computed and used as training data
88 for DIISCO (**Fig. 1A**). The cell type dynamics can be in the form of cell counts at each time point
89 or standardized proportions of each cell type, i.e. normalized by total cells in the sample collected
90 at each time point. Using proportions is often useful in complex patient data where the sampling
91 and quality of biopsies are inconsistent over time points ([Maurer et al., 2024](#)).

92 Our first assumption is that cell-cell communication, especially if associated with response to
93 external perturbation, can be reflected in compositional shifts in cell states. In other words, a
94 positive or negative temporal correlation between two cell states may be indicative of an activating
95 or inhibitory interaction between them, respectively. Our second assumption is that differential gene
96 expression of receptor-ligand complexes by these correlated cell types reinforces the likelihood of
97 direct cell-cell communication. To improve predictive power in time intervals with low cell numbers,
98 we integrate time-series data and encode temporal dependencies between interaction networks at
99 different time-points. By simultaneously fitting the model to all detected cell states and all time-
100 points, the algorithm effectively identifies the best sender cell state communicating with each receiver
101 cell state, and leverages data observed in other time points, particularly the closest ones to improve
102 prediction at a given timepoint. The output of DIISCO is two-fold. It includes predicted cell type
103 dynamics which is helpful for assessing model fit, e.g. when tuning hyperparameters. Additionally,
104 DIISCO outputs a time-series interaction matrix that reveals which cell-cell interactions are evolving
105 with time (**Fig. 1A**).

106 At its core, DIISCO utilizes a generative model. To capture the temporal dynamics of cell types,
107 i.e. changes in their frequency over time, while addressing the challenge of varying time intervals,
108 we deploy Gaussian Process regression models ([Wilson et al., 2011](#)) (**Methods**). Gaussian pro-

109 cesses (GPs) provide sufficient flexibility with nonparametric function learning, and therefore do
110 not require any knowledge of form or rate of changes of cell types, thus expanding their applica-
111 bility. They have been proven successful in integrating time-series single-cell datasets (Lönnberg
112 et al., 2017), and in identifying key cell states with distinct temporal dynamics shaping response
113 to immunotherapy in human leukemia (Bachireddy et al., 2021). By utilizing GPs, which encode
114 temporal dependencies between all pairs of time points, we expand the utility of the model not only
115 to controlled experimental settings but also to scenarios with variable timing, e.g. patient data.

116 To encode dynamic interactions between cell types (Fig. 1B), we draw inspiration from Gaus-
117 sian Process Regression Networks (GPRNs) which have been previously applied to gene expression
118 dynamics as well as datasets in finance, physics, geostatistics, and air pollution (Wilson et al., 2011;
119 Li et al., 2020). GPRNs are Bayesian multi-output regression networks that leverage the flexibility
120 and interpretability of GPs as well as structural properties of neural networks. The ability to capture
121 highly nonlinear and time-dependent correlations between outputs makes GPRNs ideal for learning
122 complex cell-cell interactions and their variability over time (Fig. 1C; Methods). While previous
123 methods have applied GPs to learning cell-type dynamics in time-series single-cell data (Bachireddy
124 et al., 2021), our method is the first to utilize a GPRN framework for learning interactions between
125 cell types, rather than learning the dynamics of each cell type independently.

126 Finally, DIISCO utilizes an optional prior based on the expression of receptor ligands (R-Ls)
127 and learns interactions from both R-L genepairs and temporal dynamics of cell types, while reliance
128 on R-Ls can be adjusted with the prior strength (Fig. 1D; Methods). Utilizing the R-Ls is
129 beneficial for constraining the solution space of interactions and improving model identifiability and
130 robustness.

131 DIISCO recovers time-resolved interactions in synthetic data

132 We first evaluated the performance of DIISCO on synthetic data by constructing a dataset with
133 known dynamics and interactions (Methods). We observe an accurate modeling of temporal dy-
134 namics for 5 simulated cell states, even with volatile dynamics and non-uniform sampling of time-
135 points (Fig. 2A,C).

136 Through these simulations, we noted DIISCO’s ability to uncover a wide range of interac-
137 tions, including constant interactions, monotonically increasing or decreasing interactions, as well

138 as transient interactions (**Fig. 2B,D**). Distinguishing various forms of interactions is important in
139 biological data, especially in studying the impacts of perturbations and disease progression, and in
140 resolving the timing of critical crosstalk. In the case of disease progression, interactions between
141 cell types may steadily increase or decrease over time (such as in $C4 \leftarrow C0$ and $C2 \leftarrow C1$), e.g. as
142 malignant cells become more prominent or immune cells exhibit clonal expansion. Recapitulating
143 these complex interactions by DIISCO demonstrates its potential to derive insights into dynamic
144 cell communication.

145 Since sparse sampling of time-points can typically occur in real-world scenarios, particularly
146 with clinical samples, we evaluated the robustness of our method to the number of time-points.
147 We repeated the described experiment with removing a random subset of timepoints, ranging from
148 10-100% and observed sustained performance even with 70% of time-points removed (**Fig. 2E**). We
149 also tested the scalability of DIISCO by increasing the number of clusters and time points (**Fig. 2F**),
150 as well as analyzing the algorithmic complexity of DIISCO (**Methods**). Our empirical assessment
151 of scalability confirmed exponential scaling with number of cell types and time points; however we
152 still observe run times less than 5 minutes for 100 simulated clusters and 20 time points using a
153 Google Cloud machine instance with 117 GB of RAM and 30 cores (**Fig. 2D**). This scalability
154 suggests DIISCO would be able to provide insight into large-scale temporal cell atlases, should they
155 become available.

156 To further benchmark DIISCO's ability to infer temporal dynamics and interactions, we com-
157 pared DIISCO's performance to both a linear model and a rolling linear model (**Methods**). We also
158 tested the importance of the prior, by comparing to models with and without a prior incorporated.
159 By simulating various scenarios with differing time-points and noise (**Methods**), we confirmed that
160 DIISCO accurately reconstructs temporal changes, and demonstrates superior performance in pre-
161 dicting interactions compared to baseline models without the prior (**Fig. 2G, Supplementary**
162 **Tables 1-2**). The performance in predicting interactions between cell types at measured time-points
163 becomes comparable to the rolling linear model if the DIISCO prior is incorporated, underscoring
164 the impact of promoting sparsity in the interaction network. However, the baseline models are
165 yet incapable of interpolating interactions between measured time-points, limiting the evaluation of
166 interaction dynamics over time. They are also unable to identify R-Ls or gene programs correlated
167 with time-resolved cell type interactions. Overall, DIISCO performs both tasks of inferring smooth

168 time-dependent interactions without assumptions about functional form and incorporating prior
169 knowledge in an integrated Bayesian framework, while quantifying uncertainty and enabling down-
170 stream analysis of underlying mechanisms. This is an essential feature for biological applications
171 and hypothesis generation for future investigations.

172 **DIISCO characterizes dynamic interactions between CAR-T and lymphoma cells**

173 To demonstrate an application of DIISCO to biological data, we generated single-cell data from
174 a controlled *in vitro* experimental setting. Specifically, we co-cultured GFP-transduced anti-CD19
175 chimeric antigen receptor (CAR) T cells together with MEC1 cells (Stacchini et al., 1999) - a B cell
176 (chronic lymphocytic leukemia [CLL]) leukemia cell line expressing *CD19* - as the CAR-T cell target
177 (Fig. 3A; Supplementary Fig. S1A-C; Methods). We confirmed dose response activation
178 (cytotoxicity) of T cells by quantifying the percentage of remaining MEC1 cells. This showed a
179 reduction in MEC1 cell survival starting from 50 – 60% at an effector-to-target ratio of 0.125 to
180 survival of < 5% at an effector-to-target ratio of 4 (Supplementary Fig. S1D). We profiled
181 4 biological replicates with scRNA-seq at 10 time-points spanning 24hrs, thereby obtaining high-
182 quality data for 49,283 total cells (Supplementary Table 3). The data shows compositional shifts
183 with time, motivating the use of this dataset as a test case for investigating temporal interactions
184 with DIISCO (Fig. 3B).

185 We preprocessed this data by defining major cell types from the combination of all replicate
186 experiments to increase statistical power. Through clustering and examining expression of curated
187 gene sets, we identified 4 major cell types (metaclusters): cancer cells, exhausted $CD8^+$ T cells,
188 activated $CD8^+$ T cells, and other $CD8^+$ T cells showing neither activated nor exhausted markers.
189 MEC1 cancer cells were annotated based on the expression of *CD19* and *CD79A*. T cells were
190 annotated based on the expression of *CD3E*, *CD3D*, and *CD8A*. Activated T cells were defined
191 by expression of *CD69*, *CD27*, and *CD28*, while exhausted cells were defined by expression of
192 *TIGIT*, *PDCD1*, *TGFB1*, and *LAG3* (Fig. 3C-E). Clusters that were positive for both T cell and
193 MEC1 gene markers were removed as doublets. We acknowledge that doublets could also contain
194 interacting cells. However, since we only obtain one measurement of receptor or ligand gene, our
195 current method (as well as existing methods) cannot resolve them. Future extensions deploying
196 mixture models could help deconvolve doublets.

197 After cell type annotation, proportions were calculated at each time point, and DIISCO was
198 trained on each experiment separately (**Supplementary Fig. S2A,C**). To construct the prior for
199 interactions, we obtained a set of 8,234 literature-curated receptor-ligand (RL) pairs from Omni-
200 Path, a database of cell signaling prior knowledge (Türei et al., 2016) and summarized the number
201 of R-Ls with differential expression between each pair of cell types (**Fig. 3F**; **Methods**).

202 Applied to the CAR-T and MEC1 data, DIISCO learned the proportions of cell types, highlight-
203 ing the expected decrease in cancer cells over time and the increase in exhausted T cells (**Fig. 4A**;
204 **Supplementary Fig. S2A,C**). We also inferred interactions between cell types and specifically
205 observed strong negative interactions predicted between cancer cells and exhausted CAR-T cells,
206 as well as between activated and exhausted T cells (**Fig. 4B,C**; **Supplementary Fig. S2B,D**).
207 Investigating the dynamics of interactions $W(t)$ over time, as expected, we predicted an increase in
208 the strength of the interaction ($|W|$) with co-culture time (**Fig. 4C**) between exhausted T cells and
209 MEC1 cells, as well as in exhausted T cells interacting with activated T cells, which was direction-
210 ally specific. The former recapitulated the targeting of cancer cells by T cells and the latter may be
211 due to phenotypic shifts from activated T cells becoming more exhausted or terminally differenti-
212 ated over time (Bachireddy et al., 2021). When comparing DIISCO results across experiments, we
213 note that the predicted interactions (W) between cell types averaged over time, remain consistent
214 for the strongest positive and negative interactions (**Supplementary Fig. S2E**). Furthermore,
215 the main interaction links between Exhausted T cell - MEC1 and Exhausted - Activated T cells
216 exhibit the same time-varying dynamics across experiments, demonstrating DIISCO's robustness
217 and reproducibility across biological replicates (**Supplementary Fig. S2F-G**). One benefit of
218 DIISCO is its ability to provide uncertainty estimates in interaction predictions, and we note that
219 the uncertainty, as defined by the 85% confidence interval, increases after 12 hours, due to increased
220 sparsity in collected timepoints (**Supplementary Fig. S3**).

221 The ability to predict how interactions between exhausted T cells and MEC1 cells evolve with
222 time is a unique feature of DIISCO, whereas other existing methods are not able to achieve such
223 time-resolved predictions. Indeed, we observed a positive correlation between predicted interaction
224 strength and co-culture time (**Fig. 4C**), in line with the cytotoxicity of T cells, i.e. their increased
225 ability to kill cancer cells.

226 Additionally, we assessed the sensitivity of DIISCO to the interaction prior by changing the

227 interaction score threshold that we used for quantifying the number of possible R-L complexes
228 associated with a pair of cell states. A lower threshold would lead to a larger solution space,
229 while higher thresholds emphasize clusters with the largest number of expressed R-L genes. We
230 noted that the average interaction strength predicted by DIISCO remained stable, excluding the
231 interactions that drop out with higher thresholds (**Fig. 4D**). Importantly, the ranking of most
232 strongest predicted interactions remained stable (**Fig. 4E**).

233 To assess the sensitivity of DIISCO to the number of cells, we downsampled the cells in this
234 dataset and observed robust ranking of interactions even when cells are downsampled to 30% of
235 the original numbers, with only minor changes when downsampling 40 – 50% of cells (**Fig. 4F-H**;
236 **Supplementary Fig. 4A**). To additionally test sensitivity to user input, we also downsampled
237 the time-points in this dataset (**Supplementary Fig. 4B**). DIISCO recovers similar dynamics
238 even with 50% of time-points dropped. Tracking the average interaction strengths over time, we
239 see robust estimations even with 30% of time points dropped (**Supplementary Fig. 4C**). This is
240 also evident in the time-varying dynamics of these interactions (**Supplementary Fig. 4D,E**). We
241 additionally sought to test sensitivity to clustering techniques, as users may utilize different pre-
242 processing pipelines. We first tested DIISCO’s performance on the individual Phenograph clusters
243 without merging them into metaclusters. The results show MEC1 cells (clusters 10, 17, 22, 23) have
244 a decrease in proportion after 10 hours post-co-culture (**Supplementary Fig. 5A**). Activated T
245 cells (clusters 3, 12) show higher proportions early in the experiment and then decrease over time.
246 This complements the dynamics of exhausted T cells (clusters 9, 15, 26) which are increasing over
247 time.

248 Examining the average W interactions over time, C10→C26 and C10→C9 are the strongest
249 negative interactions (**Supplementary Fig. 5B-C**) These are both MEC-Exhausted Tcell links
250 consistent with our previous results at the level of metaclusters. The strongest positive interactions
251 belong to C23→C9, C9→C23, and C26→C9. These are MEC-Exhausted T cell and Exhausted
252 T cell -Exhausted T cell interactions. These results demonstrate DIISCO’s robustness to various
253 clustering methods and varying data quality. One benefit to combining clusters into metaclusters
254 that define individual cell types, is the ability to remove any self-interactions. With multiple clusters
255 representing exhausted T cells, we see interactions between different exhausted T cell clusters arise.
256 Although there are cases where this may be important to study, DIISCO has been built to study

intercellular interactions between different cell types, instead of within them. We also demonstrate DIISCO's robustness to clustering method by re-processing the data following SCANPY's pipeline, including Leiden clustering to define cell types (**Methods**). We see similar results in both dynamics and predicted interactions (**Supplementary Fig. 5D-F**).

DIISCO outperforms existing methods in identifying cell communication mediated by signaling molecules

To investigate mechanisms underlying the interaction between MEC1 cells and exhausted T cells in our *in vitro* experiment, we calculated the correlations between different R-L gene pairs and the learned dynamic interaction (**Fig. 5A**). For calibration, we first confirmed that *CD19*, the target of the engineered CAR, is highly correlated with the interaction from exhausted T cells to MEC1 cells, as expected (**Fig. 5A**). Examining the MEC1 \rightarrow Exhausted interaction, *CD86-CTLA4* and *CD80-CTLA4* were the top R-L pairs ranked by ligand correlation (**Fig. 5A**). *CTLA4* is an established marker of T cell exhaustion, and *CD80* and *CD86* are costimulatory molecules that are expressed in malignant lymphocytes (including B cells) in several hematologic diseases ([Dorfman et al., 1997](#); [Vyth-Dreese et al., 1998](#); [Delabie et al., 1993](#)). Ranked by the highest average correlation, *ICAM1-IL2RA* was the top predicted R-L pair. *ICAM1* is a known regulator of inflammatory response and is elevated in CLL patients with more severe disease progression ([Molica et al., 1995](#); [Musolino et al., 1996](#); [Bui et al., 2020](#)).

Finally, we benchmarked the predicted DIISCO R-L interactions against other methods including CellChat ([Jin et al., 2021](#)) and CellPhoneDB ([Efremova et al., 2020](#)). We applied CellPhoneDB and CellChat to log-normalized expression data from all time points. We excluded any interactions within the same cluster (i.e. MEC1 \rightarrow MEC1). R-L pairs were filtered based on p-value ($p < 0.05$), and we identified 260 significant pairs using CellPhoneDB and 180 significant interactions using CellChat.

To compare these results to DIISCO-predicted interactions, we calculated the correlation between the predicted receptor and ligand expression over all time points. Our rationale is that if R-L protein complexes mediate cell-cell interaction, their expression levels on the corresponding sender and receiver cell types will likely change concomitantly. Otherwise, the genes are less likely to be involved in the cellular interaction and could rather be intrinsic markers of the cell states. We

286 observed a significantly higher Pearson’s correlation for R-Ls in DIISCO-predicted interactions than
287 those predicted by other methods (**Fig. 5B**). Since changes in the expression of receptor genes on
288 the receiver cell type may not be linearly associated with the corresponding ligand expression on the
289 sender, we also calculated Spearman’s correlation, again demonstrating a significant improvement
290 with DIISCO (**Fig. 5B**). Although all 3 methods identified the *CD80/CD86-CTLA4* interactions,
291 only DIISCO predicted the *ICAM1-IL2RA* interaction, which is the one with the most time-varying
292 expression. Note that temporal changes in expression of R-L genes is not used in the DIISCO prior.
293 Our results thus confirm the ability of DIISCO to identify a monotonic increase in the expression
294 of R-L pairs underlying cell-cell interactions.

295 Further examining the overlap between methods, we noted that the predicted interactions shared
296 between DIISCO and CellChat are the most correlated by both Spearman’s correlation and mutual
297 information as another metric, while the interactions predicted by both DIISCO and CellphoneDB
298 are most correlated using the Pearson’s correlation test (**Fig. 5C**). Combined, these results confirm
299 DIISCO’s ability to identify cell-cell communication that can be supported by co-expressed R-L
300 gene pairs, from time-series single-cell data.

301 As DIISCO learns interactions from the integration of time-series data, we further compared
302 DIISCO to cellphoneDB applied to different time-points. Due to low numbers of cells in metaclusters
303 in individual time-points, we were unable to apply cellphoneDB to each time point separately.
304 Instead, we combined the first 5 and last 4 time points into ‘early’ and ‘late’ time intervals to obtain
305 pseudo-dynamic interactions. Identifying R-L pairs that were only predicted in the ‘late’ bucket
306 suggests that these interactions are growing in strength over time. Predicted R-L interactions
307 between MEC1–Exhausted cells found with both DIISCO and the ‘late’ bucket in cellphoneDB
308 include *TNF-ICOS*, *FAM3C-PDCD1*, and *FAM3C-LAMP1*. *ICOS* is known to be expressed on
309 activated T cells, and it has been investigated as a costimulatory domain for CAR-T cell therapy (([He
310 et al., 2022](#))). High expression of *TNF* in CLL cells has been associated with poor prognosis, and
311 *TNF* has been suggested as a potential target for CLL immunotherapies (([Dürr et al., 2018](#))). Even
312 with the bucketing approach cellphoneDB did not predict *CD80/CD86-CTLA4* interactions, which
313 have strong literature support for their importance in CLL (([Dorfman et al., 1997](#); [Vyth-Dreese
314 et al., 1998](#); [Delabie et al., 1993](#))). CellphoneDB also did not identify the *ICAM1-IL2RA* interaction.
315 This suggests that incorporating temporal dynamics is crucial for identifying R-L interactions most

316 relevant to the biological system.

317 Discussion

318 As longitudinal single-cell datasets become more prevalent, we believe DIISCO can provide a rigor-
319 ous and flexible framework for characterizing cell-cell communication and its temporal variability,
320 aiding in the understanding of disease progression and impact of treatments or perturbations in
321 complex biological systems.

322 We demonstrate the performance of DIISCO in simulated data as well as cancer-immune cell
323 interaction data. In particular, we show how the integration of time-series data and prior knowledge
324 of protein complexes in a probabilistic model leads to achieving dynamic intercellular interactions.
325 The ability to infer the sign and change in strength of interactions with time is not attainable with
326 previous methods and is crucial for studying the impact of perturbations such as treatment. In
327 addition, DIISCO provides insight into signaling mechanisms mediating dynamic interactions.

328 The advantage of the probabilistic framework is that with very few time points or long time
329 intervals, DIISCO will present high uncertainty for estimates. We also show high accuracy in
330 synthetic data for predictions even with sparse sampling of time points. While the interaction prior
331 impacts model identifiability, we showed that the strongest inferred interactions are robust to the
332 prior strength.

333 The choice of hyperparameters is essential for achieving interpretable dynamics. We thus provide
334 comprehensive guidance for the choice of hyperparameters according to data quality and sampling
335 rate in Supplementary Information Section [D](#). Additionally, spurious correlations may emerge when
336 using cell type proportions due to the constraint of having all points in the simplex. Supplementary
337 Information section [E](#) includes a short discussion on this issue.

338 As DIISCO assumes that cellular interactions lead to shifts in the cell state composition in the
339 system, it may not be an appropriate method if no changes in cell state proportions or numbers are
340 observed over time. This may be the case with communication mediated by cells exhibiting static
341 proportion. However, compositional shifts frequently occur with perturbations such as therapy or
342 external stimuli, and are particularly relevant in clonally expanding lymphocytes driving immune
343 response, e.g. in hematological malignancies such as leukemia. We recently showed that DIISCO can

344 resolve time-varying dynamics associated with response to therapy in single-cell data collected from
345 relapsed leukemia patient samples (Maurer et al., 2024). This dataset involves 74 longitudinal bone
346 marrow samples from 25 heterogeneous relapsed leukemia patients. Furthermore, the number of cells
347 ranged from 144 to 14,584 high-quality cells across samples and our results demonstrate DIISCO’s
348 robustness to unbalanced datasets. DIISCO revealed a cascade of immune interactions centered
349 around a cytotoxic T-cell subtype that expands with therapy, and further identified potential R-L
350 complexes associated with predicted interactions.

351 To address limitations in relying on changes in cell type composition in other systems, DIISCO
352 can potentially be adapted to learn temporal correlations between modules of co-expressed genes
353 instead of cell state proportions. Furthermore, there is an inherent limitation in using R-L databases
354 to learn interactions. Although DIISCO addresses this limitation through binarization, the lack
355 of context-dependent information in these databases requires the user to interpret the predicted
356 interactions and downstream gene networks relevant to the context. Identified interactions should
357 also be validated through literature searches or follow-up experiments.

358 Future application of DIISCO to other clinical datasets can elucidate cell-cell communication
359 underlying response or resistance to treatments such as immunotherapy. Deciphering the mecha-
360 nisms of response and lack of response to therapy allows for more patient-specific therapeutics and
361 offers the opportunity to reverse-engineer new therapies for improved efficacy.

362 We envision multiple directions for building upon this work. Notably, for clinical samples,
363 incorporating priors that account for sample size (i.e., total cells) could improve robustness by down-
364 weighting the influence of samples with very few cells. Recent advances in spatial transcriptomics
365 also offer an opportunity to expand DIISCO and infer interactions from both temporal and spatial
366 dynamics by integrating spatial co-localization information.

367 **Methods**

368 **Notations**

369 We assume that we have N cell types with their frequencies measured at time points t_1, \dots, t_N .
370 We define $y(t_i)$ as a K -dimensional vector of observations at time t_i where the k -th dimension
371 corresponds to the frequency of the k -th cell type. Additionally, we assume we have a set of M

372 unobserved time points t_{N+1}, \dots, t_{N+M} , placed anywhere on the time axis, for which we would like
 373 to infer (interpolate) the cell type values $y(t_{N+1}), \dots, y(t_{N+M})$. We denote the set of all time points
 374 as $\mathcal{T} = \{t_1, \dots, t_{N+M}\}$ and call \mathcal{T}_u the set of unobserved time points $\mathcal{T}_u = \{t_{N+1}, \dots, t_{N+M}\}$ and
 375 \mathcal{T}_o the set of observed time points $\mathcal{T}_o = \{t_1, \dots, t_N\}$. We use the convention of \cdot_u and \cdot_o to denote
 376 unobserved and observed variables respectively. In the remainder, for ease of exposition, we will
 377 refer to $y(t_i)$ as proportions with the understanding that either proportions or cell counts could be
 378 used, although the results should be interpreted in a different manner depending on the value used.

379 In addition to these features, we have a binary matrix Λ of size $K \times K$ where $\Lambda_{k,k'} = 1$ indicates
 380 that the k -th cell type might interact with the k' -th cell type and $\Lambda_{k,k'} = 0$ indicates that they
 381 don't. We allow for non-symmetric matrices to allow for directionality in interactions. In practice,
 382 we obtain this matrix from measurements of expression of known receptor-ligand complexes.

383 Model Specification

384 DIISCO is a generative model that assumes cell type frequencies, denoted as $\hat{y}(t_i)$, are derived from
 385 the following process (**Fig. 1B**):

- 386 1. For every time point, we sample a set of latent features, $f(t_i) \in \mathbb{R}^K$ where every feature,
 387 i.e every coordinate of $f(t_i)$, is a Gaussian process. We call this set $\mathcal{F} = \{f(t_i) \mid t_i \in \mathcal{T}\}$
 388 and let \mathcal{F}_o and \mathcal{F}_u denote the set of latent features at observed and unobserved time points
 389 respectively.
- 390 2. Similarly, we sample at each time point an interaction matrix $W(t_i) \in \mathbb{R}^{K \times K}$ where we also
 391 assume that each of the $K \times K$ coordinates of $W(t_i)$ is a Gaussian process across time. We
 392 call this set $\mathcal{W} = \{W(t_i) \mid t_i \in \mathcal{T}\}$ and let \mathcal{W}_o and \mathcal{W}_u denote the set of interaction matrices
 393 at observed and unobserved time points respectively.
- 394 3. Finally, we sample the standardized cell type proportions $\hat{y}(t_i) \in \mathbb{R}^K$. We do this by sampling
 395 from a multivariate Gaussian with mean $W(t_i)f(t_i)$ and covariance $\sigma_y^2 I$. In other words:

$$\hat{y}(t_i) = W(t_i)f(t_i) + \epsilon(t_i) \quad (1)$$

396 where $\epsilon(t_i) \sim \mathcal{N}(0, \sigma_y^2 I)$ represents a zero-centered Gaussian noise process. We use $\mathcal{Y} =$

397 $\{\hat{y}(t_i) \mid t_i \in \mathcal{T}\}$ to denote the set of all standardized cell type proportions across all time
 398 points with \mathcal{Y}_o and \mathcal{Y}_u having the same meaning as before. We also allow for the inclusion of
 399 a bias term $b(t)$ such that $Y(t) = W(t)f(t) + b(t) + \epsilon(t)$ where $b(t)$ is centered at 0 and has a
 400 kernel like that of $W(t)$ but without any interaction regularization. For brevity, we omit it as
 401 it is equivalent to extending the model dimension by one, ignoring the last coordinate of $y(t)$,
 402 and setting the last coordinate of $f(t)$ to be a GP centered at 1 with infinite length-scale.

403 **Figure 1C** depicts this process graphically and **Algorithm 1** details the generative process. The
 404 arrows $\mathcal{W}_o \rightarrow \mathcal{W}_u$ and $\mathcal{F}_o \rightarrow \mathcal{F}_u$ represent tractable distributions that can be computed analytically
 405 and can be sampled due to the properties of Gaussian processes. Thus, the model only requires
 406 tractable operations that lead to the joint distribution described. DIISCO currently ignores the
 407 original space that the data lies in and makes the simplifying assumption that $y(t)$ can be treated
 408 as a vector in \mathbb{R}^k rather than on the simplex or the space of positive integers. Although these
 409 assumptions aid greatly in the interpretability of the latent variables, further improvements using
 410 distributions that truly match the real support of the data would lead to better uncertainty estimates
 411 and predictions.

Algorithm 1 Generative Process used by DIISCO

1: **Input:** Set of time points \mathcal{T} , Number of latent features K , Noise covariance σ_y^2 .

Sampling of Latent Features

2: **for** each feature $k \in \{1, \dots, K\}$ **do**
 3: Sample $f_k(t) \sim \mathcal{GP}(m_k^f(t), K_k^f(t_i, t_j))$
 4: **end for**

Sampling of Interaction Matrix

5: **for** each feature $k \in \{1, \dots, K\}$ **do**
 6: **for** each feature $k' \in \{1, \dots, K\}$ **do**
 7: Sample interaction $W_{k,k'}(t) \sim \mathcal{GP}(0, K_{k,k'}^W(t_i, t_j))$
 8: **end for**
 9: **end for**

Sampling of Observed Values

10: Sample a K -dimensional Gaussian noise process $\epsilon(t) \sim \mathcal{N}(0, \sigma_y^2 I_K)$
 11: Compute standardized cell type proportions: $\hat{y}(t) \leftarrow W(t)f(t) + \epsilon(t)$

412 **Model Interpretation.**

413 The latent variable $W_{i,j}(t)$ represents the direction and effect of intercellular interaction (signaling
 414 communication) from cell type j to cell type i at time t . In particular, $W_{i,j}(t) > 0$ represents an
 415 activating effect, $W_{i,j}(t) < 0$ denotes inhibitory impact, and $|W_{i,j}(t)|$ reflects the strength of the
 416 interaction. $f(t)_i$ is a latent variable that represents the normalized proportion of cell type i at
 417 time t (**Fig. 1B**). DIISCO focuses on identifying interactions between different cell states. Thus, in
 418 constructing the prior for W , we penalize self-interactions $W_{i,i}$, such that $W_{i,j}$ can be interpreted as
 419 the impact of other cell types $j \neq i$ on the dynamics of cell type i . We justify why this interpretation
 420 is reasonable, given our choice of priors below.

421 **Prior Distribution over \mathcal{F} .**

422 Intuitively, we aim for the latent features to align closely with standardized cell type proportions so
 423 that $W(t)$, with suitable restrictions on the diagonal, learns to capture the interactions between cell
 424 types by predicting the standardized proportion of one cell type given the standardized proportions
 425 of the rest. We achieve this by first defining for every feature an auxiliary zero-mean Gaussian
 426 process (GP) on which we perform inference. Formally, for every $k \in \{1, \dots, K\}$ we define an
 427 auxiliary GP with covariance function K^f given by:

$$K^f(t_i, t_j) = v_f \exp\left(-\frac{(t_i - t_j)^2}{2\tau_f^2}\right) + \sigma_f^2 \delta_{ij}. \quad (2)$$

428 where δ_{ij} is the Kronecker delta function, and v_f , τ_f , and σ_f are shared hyperparameters denoting
 429 the variance of the latent features, the length scale of the latent features and the noise of the
 430 latent features, respectively. We then update this auxiliary GPs using the observations $\hat{y}_k(t_i)$ at
 431 the observed time points $t_i \in \mathcal{T}_o$ which provides us with a posterior Gaussian Processes $\mathcal{GP}(\mu_k^f, K_k^f)$
 432 that we use as the prior for the Gaussian Process corresponding to feature $f_k(t)$ in Algorithm **1**.

433 **Prior Distribution over \mathcal{W} .**

434 To further limit the solution space, and improve model robustness and interpretability, we set two
 435 constraints on the sampling process of W . First, we set off-diagonal elements to zero if the cluster
 436 pairs do not express any complementary receptor-ligand pairs and second, we zero out the diagonals

437 when a row has at least one other non-zero entry. In the case when we are dealing with proportions
 438 and not raw counts this also ensures that we avoid a trivial solution due to the $\sum_k y_k(t) = 1$.
 439 Formally, we achieve this by sampling $W(t)$ so that for $k, k' \in \{1, \dots, K\}$.

$$W_{k,k'}(t) \sim \mathcal{GP}(0, K_{k,k'}^W(t, t)) \quad (3)$$

440 where

$$K_{k,k'}^W(t, t') = \begin{cases} v_W \exp\left(-\frac{(t-t')^2}{2\tau_W^2}\right) + \sigma_W^2 & \text{if } k \neq k' \\ 0 & \text{if } k = k' \text{ or } \Lambda_{k,k'} = 0 \end{cases} \quad (4)$$

441 and v_W , τ_W , and σ_W are shared hyper-parameters, retaining the same interpretations as before.
 442 To construct Λ , we scan for complementary expression of known RL pairs, i.e. when the sending
 443 cluster expresses a ligand at a defined threshold and the receiving cluster expresses the comple-
 444 mentary receptor at a similarly defined threshold (**Fig. 1D**). This threshold is user-specified, as
 445 different genes are captured at different rates in sequencing data and a single threshold may not be
 446 an accurate representation of relative expression across all genes.

447 We then quantify the number of these interactions expressed by cluster pairs. The number of
 448 RL pairs does not necessarily determine the strength of interaction, and a single complementary
 449 RL pair could be biologically important. To account for this, we set a binarization threshold. The
 450 binarization threshold can be set by users and may be datatype-specific. A very high threshold leads
 451 to a prior that is too sparse and may lead to losing potentially relevant interactions, whereas a very
 452 low threshold may lead to spurious interactions. The threshold is user-specified and determines the
 453 sparsity of the prior during the binarization step.

454 To demonstrate the robustness of predicted interactions to the threshold, we performed addi-
 455 tional sensitivity analysis by dropping 30-70% of the R-L pairs in the Omnipath R-L database.
 456 When we drop different percentages of R-L pairs, we obtain a similar distribution of interaction
 457 scores (Supplementary Fig. 6A-C). By specifying a threshold guided by the knee point of these
 458 distributions, we achieve the same prior using 30% or 70% of the data. By changing the threshold
 459 to account for downsampled or incomplete interactions, we can retain flexibility in the model and
 460 utilize a consistent prior. Unfortunately, similar to current interaction methods like CellphoneDB

461 or CellChat, if there is a bias in the database where certain cell types are underrepresented, we are
 462 unable to capture that in the predicted results. Future databases expanding these interactions can
 463 improve results obtained with DIISCO.

464 By binarizing the RL interaction matrix, we allow for more model flexibility while also limiting
 465 the solution space to exclude clusters with no complementary RL expression. This final binary
 466 matrix is defined as Λ , and as shown in equation 4, the value of $\Lambda_{k,k'}$ determines whether the
 467 model allows for a possible interaction between cell types k and k' . In practice, we build the prior
 468 using OmnipathDB, a database used by more traditional interaction methods like cellphoneDB
 469 ((Türei et al., 2016)). However, it is important to note that R-L databases lack context-dependent
 470 information and are often incomplete with many interactions having not been characterized yet in
 471 literature.

472 Inference

473 Due to the complex nature of the model, it is not possible to perform inference analytically. Instead,
 474 we deploy a two-step approximate inference method combining both analytic and approximate
 475 techniques.

476 Specifically, we: (1) perform approximate inference to obtain samples from an estimate of the
 477 posterior distribution $p(\mathcal{W}_o, \mathcal{F}_o | \mathcal{Y}_o)$; and (2) perform ancestral sampling and standard GP condi-
 478 tioning to obtain an approximation to the posterior distribution $p(\mathcal{W}_u, \mathcal{F}_u, \mathcal{Y}_u | \mathcal{Y}_o, \mathcal{W}_o, \mathcal{F}_o)$. Sup-
 479plementary Information Section B provides a justification for this approach. Below we describe in
 480 detail how we perform each of these steps.

481 Approximate Inference.

482 To approximate $p(\mathcal{W}_o, \mathcal{F}_o | \mathcal{Y}_o)$ we use variational inference implemented using Pyro (Bingham
 483 et al., 2019), a probabilistic programming language written in Python. Within this framework, we
 484 define a parametrized distribution $q_\phi(\mathcal{W}_o, \mathcal{F}_o)$ and then optimize the parameters ϕ to maximize an
 485 estimate of the evidence lower bound (ELBO) (Blei et al., 2017) via a gradient descent algorithm.
 486 In the situation where the hyper-parameters are fixed, this is equivalent to minimizing the KL
 487 divergence $\text{KL}(q_\phi(\mathcal{W}_o, \mathcal{F}_o) || p(\mathcal{W}_o, \mathcal{F}_o | \mathcal{Y}_o))$.

488 In this case the ELBO is given by

$$\mathcal{L}(\phi) = \mathbb{E}_{q_\phi(\mathcal{W}_o, \mathcal{F}_o)} [\log p(\mathcal{Y}_o, \mathcal{W}_o, \mathcal{F}_o) - \log q_\phi(\mathcal{W}_o, \mathcal{F}_o)] \quad (5)$$

489 and we define $q_\phi(\mathcal{W}_o, \mathcal{F}_o)$ as a multivariate Gaussian factorized by:

$$q_\phi(\mathcal{W}_o, \mathcal{F}_o) = \prod_{k, k' \in \{1, \dots, K\}} \mathcal{N}(W_{k, k'}(\mathcal{T}_o) \mid \hat{\mu}_{k, k'}^W, \hat{\Sigma}_{k, k'}^W) \prod_{k \in \{1, \dots, K\}} \mathcal{N}(f_k(\mathcal{T}_o) \mid \hat{\mu}_k^f, \hat{\Sigma}_k^f) \quad (6)$$

490 where $\hat{\mu}_{k, k'}^W \in \mathbb{R}^n$ and $\hat{\Sigma}_{k, k'}^W \in \mathbb{R}^{n \times n}$ are the mean and covariance of $W_{k, k'}(\mathcal{T}_o)$, $\hat{\mu}_k^f$ and $\hat{\Sigma}_k^f$ are the
 491 mean and covariance of $f_k(\mathcal{T})$, $W_{k, k'}(\mathcal{T}_o)$ denotes the vector of values of $W_{k, k'}(t)$ for $t \in \mathcal{T}_o$ and
 492 $f_k(\mathcal{T}_o)$ denotes the vector of values of $f_k(t)$ for $t \in \mathcal{T}_o$.

493 In other words, we assume that the latent features and the interaction matrix are independent
 494 of each other, but they are dependent across timepoints, and this dependency is captured by the
 495 mean and covariance of the Gaussian distribution. In practice, we parameterize the Cholesky
 496 decomposition of the covariance matrix rather than the covariance matrix itself and use Adam
 497 (Kingma and Ba, 2014) to optimize the parameters ϕ . Due to the amount of computation required
 498 for using this variational family, we also provide in the package the option to use a mean-field guide
 499 where each variable is fully independent from each other and is parameterized by a one-dimensional
 500 Normal distribution, where $q_\phi(\mathcal{W}_o, \mathcal{F}_o) = \prod_{z \in \mathcal{W}_o \cup \mathcal{F}_o} q(z \mid \mu_z, \sigma_z)$. We refer to the family with the
 501 time-wise dependency structure as the partially factorized variational family, and the one with a
 502 full diagonal covariance as the fully factorized variational family.

503 To perform optimization, we used an expectation with the form $\mathbb{E}_{q_\phi(Z)}[h_\phi(Z)]$ where $Z =$
 504 $(\mathcal{W}_o, \mathcal{F}_o)$ and h represents the function inside of the expectation in equation 5. This is problematic
 505 for taking the gradient with respect to ϕ because it appears both in the distribution with respect
 506 to which we are taking the expectation and in h . However, using the fact that if $L = \text{Cholesky}(\Sigma)$,
 507 $\epsilon \sim \mathcal{N}(0, I_d)$ and $z = \mu + \Sigma\epsilon$ then z must be distributed as $\mathcal{N}(\mu, \Sigma)$, it is easy to see that one
 508 can rewrite the expectation as $E_{\mathcal{D}(\epsilon)}[h(z(\epsilon, \phi))]$ where \mathcal{D} is a multivariate normal distribution with
 509 identity covariance and $z(\epsilon, \phi)$ maps this random variable to the equivalent Z values using the
 510 above approach. We use this reparametrization trick (Kingma and Welling, 2022) to construct and
 511 estimate the gradient of the ELBO. Supplementary Information Section C outlines the inference

512 algorithm and provides details of ancestral sampling.

513 **Algorithmic Complexity and Scalability**

514 An important consideration for Gaussian Process-based models is their scalability and time com-
 515 plexity. For DIISCO, using either variational family, the computational complexity of approximate
 516 inference is of the order $O(|\mathcal{T}_o|^3 K^2)$ per gradient step and the exact conditioning step leads to a
 517 computational complexity of $O(K^2(|\mathcal{T}_o|^3 + |\mathcal{T}_o|^2 |\mathcal{T}_u|))$ for either sampling or computing the means.
 518 Supplementary Information Section [F](#) details which exact operations lead to the above bounds.

519 Nevertheless, for most of the datasets that could appear in practice the algorithmic complexity
 520 is not an issue, specially when using the fully factorized normal guide. To demonstrate this, we
 521 ran DIISCO on various simulated datasets with different sizes of \mathcal{T}_o and K to benchmark the
 522 performance. Specifically, we constructed the datasets by sampling the K Gaussian Processes with
 523 half of the processes being independently sampled and the other half being a linear combination of
 524 the independent ones. The values for the linear combination were also sampled from a GP with 10
 525 times the length scale of the independent ones, which was set to 1. To simulate sparsity for every
 526 non-independent processes we selected at random a number between 0 and $\text{floor}(K/2)$ and then
 527 proceeded to zero out that many values in the linear combination. The observed time points were
 528 sampled uniformly between 0 and 10. We then ran DIISCO for up to 50,000 iterations with early
 529 stopping if there were no improvements for over a 1,000 iterations. We conducted these experiments
 530 on a Google cloud machine instance with 117 GB of RAM and 30 cores. **Figure [2F](#)** shows that
 531 the run-time remains under 5 minutes even when fitting to up to 100 clusters and 20 time points,
 532 which are reasonable dimensions for comprehensive time-series single-cell datasets.

533 **Benchmarking with Simulated Data**

534 To understand the behavior of DIISCO under different scenarios, we conducted a benchmarking
 535 experiment using simulated data. We specifically aimed to evaluate the ability to predict interactions
 536 with nonzero strength. Details of this process are provided below.

537 **Data Generation** To define ground truth interactions for W , we simulated 7 non-zero dynamic
 538 interactions among 5 cell types using the equations below. To include cases of isolated cell types

539 that do not interact with others, we also allow non-zero diagonals in the prior for a subset of cell
 540 types. This can alternatively be captured with a bias term. In particular, we assume:

$$\begin{aligned}
 W_{0,0}(t) &= 1 & W_{2,1}(t) &= \cos((t-10)/30) \\
 W_{1,1}(t) &= 1 & W_{3,0}(t) &= \cos((t+20)/40) \\
 W_{4,0}(t) &= \cos(t/30) & W_{3,1}(t) &= \sin((t+20)/40) \\
 & & W_{4,2}(t) &= \cos((t+10)/20)
 \end{aligned}$$

541 Any interactions not listed above were set to 0. Data points were generated using the following
 542 equations:

$$\begin{aligned}
 c_0(t) &= \frac{1}{2} \cos((t+5)/3) + \cos(t/5) + \epsilon_1(t) & c_2(t) &= W_{2,1}c_1(t) + \epsilon_3(t) \\
 c_1(t) &= \sin((t+1)/2) + \cos(t/3) + \cos((t+0.5)/3) + \epsilon_2(t) & c_3(t) &= W_{3,0}c_0(t) + W_{3,1}c_1(t) + \epsilon_4(t) \\
 & & c_4(t) &= W_{4,2}c_2(t) + W_{4,0}c_0(t) + \epsilon_5(t)
 \end{aligned}$$

543 where ϵ is a noise term drawn for each time point for each cluster, and $\epsilon_i(t)$ represents noise
 544 processes. We run these simulations with two different epsilons, with a standard deviation equal to
 545 0.1 and 0.5 to represent differences in data quality. We create the dataset by sampling 100 points
 546 uniformly between 0 and 100 and then randomly downsampling the data to a range between 10-90
 547 time points. Based on this generative process, c_0 and c_1 are independent and act on c_2 , c_3 , and c_4
 548 with different interaction strengths dependent on a time-varying W . We set the following elements
 549 of the prior matrix:

$$\Lambda_{c_0,c_0} = \Lambda_{c_0,c_1} = \Lambda_{c_0,c_2} = \Lambda_{c_0,c_3} = \Lambda_{c_0,c_4} = \Lambda_{c_1,c_1} = \Lambda_{c_1,c_2} = \Lambda_{c_1,c_3} = \Lambda_{c_2,c_4} = 1 \quad (7)$$

550 All other elements of Λ are set to 0. To address potential issues with co-linearity, any cluster pairs
 551 that were correlated but not causally related through the defined equations were set to 0. We follow
 552 the guide in Supplementary Information Section [D](#). For fitting the model we let $\tau_F = 5$, $\sigma_f = 0.1$,
 553 $v_f = 3$, $\sigma_w = 0.01$, $v_w = 20$, $\sigma_y = 0.1$ and we place a gamma hyperprior on the lengthscale of W
 554 with 90 percent of the mass between 10 to 30. For this simple example, we use the DiagonalNormal
 555 guide and use Adam ([Kingma and Ba, 2014](#)) with a learning rate of 0.005

556 **Baseline Models** We compare DIISCO against two baselines.

- 557 1. **Linear Model:** We fit a linear model on the centered version of the data. For a fair compar-
558 ison, we only regress $y_k(t)$ on all $y_{k'}(t)$ such that $\Lambda_{k,k'} = 1$. We also provide a version without
559 using the prior.
- 560 2. **Rolling Linear Model:** As with the pure linear model, we fit a linear model on the centered
561 version of the data with regressors chosen via Λ . However, unlike the previous model, at every
562 observed time point t_{obs} , we fit a separate linear model containing only the data points in the
563 set $\{y_k(t_i) \mid 1 \leq i \leq N, |t - t_{\text{obs}}| < \epsilon\}$ or the closest $n_{\text{min-closest}}$ data points, whichever set is
564 larger. $n_{\text{min-closest}}$ and ϵ are hyperparameters chosen by the user. We also provide a version
565 without using the prior we construct.

566 We chose these models as they capture particular aspects of DIISCO, such as linear dependency
567 structure and, in the case of the rolling model, changing dependence through time. However, the
568 baseline models are limited in that they don't capture uncertainty in the predictions and don't
569 include a priori biases on smoothness.

570 **Converting Latent W Matrix to 0-1 Interactions** The result of DIISCO is a continuous
571 latent matrix $W(t)$. Because this matrix can be large as it scales with the square of the number of
572 cells, it is important to find a method of discretizing it automatically to determine whether a cell is
573 active or not. A helpful guideline for our experiment is to say that cell i interacts with another cell
574 j at time t if $|\mathbb{E}[W_{i,j}(t)]| \geq C\hat{\sigma}_W$, where C is a user-determined constant and $\hat{\sigma}_W$ is the standard
575 deviation of all values of the form $|\mathbb{E}[W_{k,k'}(t)]|$ with $k, k' \in \{1, \dots, K\}$ and $t \in \{t_1, \dots, t_N\}$. In our
576 experiments, we found that setting $C = 1$ is a good heuristic, but this might vary depending on
577 the sparsity assumptions that a practitioner might have about their data. We emphasize that this
578 heuristic can only be applied if the data has been scaled and centered so that the magnitude of the
579 coefficients can be interpreted meaningfully.

580 **CAR-T Data Collection**

581 CD19 CAR-T cells were generated by transducing healthy donor T cells with 3rd generation
582 lentiviral vectors encoding a bicistronic construct containing either FMC63 CD19 scFv-CD28-CD3z

583 and green fluorescent protein (GFP) or FMC63 CD19 scFv-41BB-CD3z (**Supplementary Fig.**
584 **S1A**) (Nicholson et al., 1997). Peripheral blood mononuclear cells were re-suspended at $2 \times 10^6/ml$
585 and seeded at 1ml per 24 well plate and activated with CD3/CD28 Beads. The next day, fresh me-
586 dia was added with IL2 to a final concentration of $100IU/ml$. Six hours later cells were harvested,
587 counted and re-suspended at $0.6 \times 10^6/ml$ and $0.5ml$ was seeded into a 24 well plate pre-coated with
588 retronectin (**Supplementary Fig. S1C**). $1.5ml$ of lentiviral supernatant was added to each well
589 with fresh IL2 to a final concentration of $100IU/ml$ and spun for 40 minutes at 1000G. Two days
590 later cells were harvested, re-suspended at $0.5 \times 10^6/ml$ with $50IU/ml$ of IL2 and left to expand
591 and split every 48 hours. Transduction efficiency was assessed by determining the percentage of
592 GFP+ T cells.

593 Co-cultures of CD19 CAR-T cells and MEC1 cell line (ATCC), a Chronic Lymphocytic Leukemia
594 (CLL) cell line that constitutively expresses CD19 were established at various effector-to-target ra-
595 tios and at different time points (**Supplementary Table S3**). Co-cultures were harvested together
596 and stained with hashing antibodies (Biolegend), normalized and prepared for single-cell RNA se-
597 quencing on the Chromium 10X platform. Experimental details for each of the 4 experiments found
598 in (**Supplementary Table S3**).

599 **CAR-T Data Preprocessing and Analysis**

600 Each co-culture experiment was hashed by timepoint according to **Supplementary Table S3**.
601 Demultiplexing was done in R as detailed below: All cells with less than 200 detected UMIs were
602 removed as empty droplets. For each cell, hashtag oligos (HTO) were ranked according to detected
603 counts and the standard deviation and mean for HTOs ranked 2-4 were calculated. Cells were
604 removed if the difference between HTO2 and HTO3 were within 1 standard deviation and if HTO2
605 was within 15% of the mean of HTO2-4. Finally, the top 2 HTOs for each cell were used as cell
606 identifiers and matched based on **Supplementary Table S3**.

607 All count data across all 4 experiments was aggregated and log-normalized as $(\log(0.1 + counts))$.
608 Data was visualized by UMAP, based on PCA with 8 components. Clustering was performed on 15
609 PCA components, using Phenograph (Levine et al., 2015) and a KNN with $n=15$. 30 clusters were
610 found, and then separated into 4 different metaclusters. MEC1 cells (clusters 1, 7 8, 10, 17, 22, 23,
611 24) were defined based on differential expression of *IKGC*, *CD79A*, *MS4A1*, and *CD19*. T cells were

612 defined based on differential expression of *CD3D* and *CD3E*. Exhausted T cells (clusters 0, 6, 9, 11,
 613 15, 21, 26) were defined based on *TIGIT*, *CTLA4*, *PDCD1*, *IL10*, *TGFB1*, *LAG3*, and activated
 614 cells defined based on expression of *CD69*, *CD27* and *CD28*. Any *CD8+* cells that did not express
 615 activation or exhaustion signatures were grouped into a separate fourth category (clusters 19, 28).
 616 The following clusters were removed as doublets: 2, 11, 14, 16, 20. All other clusters were removed
 617 due to low library size.

618 To construct Λ , we first obtained a set of 8,234 literature-curated receptor-ligand pairs from
 619 OmniPath, a database of cell signaling prior knowledge (Türei et al., 2016). For each cell type
 620 pair k, k' in the experiment, we quantified interactions as the number of differentially-expressed
 621 ligand genes in cell type k with their corresponding differentially-expressed receptor genes in cell
 622 type k' at each time point. These interaction count values were averaged across all time points
 623 in the experiment and then thresholded to obtain the binary interaction prior matrix Λ , where
 624 $\Lambda_{k,k'}$ signifies whether cell types k and k' can interact apriori. The threshold was chosen with a
 625 data-driven approach according to the knee-point of sorted values.

626 CAR-T Data Preprocessing - Leiden comparison

627 Count data for all CAR-T replicates was aggregated and filtered according to the SCANPY scRNA
 628 pre-processing tutorial (<https://scanpy.readthedocs.io/en/stable/tutorials/basics/clustering.html>). Cells expressing <100 genes were removed, and any genes expressed in <3 cells were removed.
 629 [html](https://scanpy.readthedocs.io/en/stable/tutorials/basics/clustering.html)). Cells expressing <100 genes were removed, and any genes expressed in <3 cells were removed.
 630 Scrublet was then used, via `scanpy.external.pp.scrublet()` function to remove doublets. Data was
 631 log normalized. The kNN neighbor graph was built on 20 PCA components and 10 neighbors, and
 632 Leiden clustering was then used to define clusters with the resolution set to 0.5. Clusters were
 633 then sorted into cell types based on gene expression. T cells were assigned based on expression of
 634 *CD3E*, and *CD3D*. Clusters 5 and 6 were designated as Exhausted T cells based on the expression
 635 of *TIGIT*, *CTLA4*, *PDCD1*, *IL10*, *TGFB1*, and *LAG3*. Clusters 7, 9, 17 were assigned as Activated
 636 T cells based on expression of *CD69*, *CD27*, and *CD28*. Clusters 0, 3, 4, 11, 14, 15 were designated
 637 as MEC1 cells based on expression of *IGKC*, *CD79A*, *MS4A1*, and *CD19*. Clusters 1, 2, 13, 16
 638 were designated as Other CD8+ T cells, and clusters 8, 10 were labeled as additional doublets
 639 and removed due to contradictory expression of both T cell and MEC1 markers. Proportions were
 640 calculated by normalizing to total numbers of cells in clusters.

641 DIISCO Design Parameters

642 *CAR-T Experiments.* Hyperparameters used for all co-culture experiments are as follows: $\sigma_F =$
 643 0.5 , $\sigma_W = 0.1$, $\sigma_Y = 0.5$, $\tau_F = 6.5$, $\tau_W = 6.5$, $v_F = 1$, $v_W = 1$. Threshold on number of interactions
 644 used for prior chosen based on midpoint for histogram of values.

645 For all CAR-T DIISCO runs, the model was trained with 10,000 iterations and a learning rate
 646 of 0.00005, and the `MultivariateNormalFactorized` guide. For predictions, 10,000 time points
 647 were sampled, and all confidence intervals were calculated as the region between the 86th and 16th
 648 percentile calculated on all predicted time points. Experiment B was excluded in comparison due
 649 to differences in Effector:Target ratio compared to all other experiments (**Supplementary Table**
 650 **S3**).

651 We used Experiment C to further evaluate the sensitivity of DIISCO to the following parameters:

- 652 1. Number of cells: Cells were subsampled by randomly removing 10%, 30%, 50%, 70%, and
 653 90% of cells from the original set of Experiment C cells. For each subsample, metacluster
 654 proportions were calculated and a separate DIISCO model was trained.
- 655 2. Number of timepoints: Separate DIISCO models were trained on the original Experiment C
 656 metacluster proportions after randomly removing proportions at 10%, 20%, 30%, 40%, and
 657 50% of the observed timepoints.
- 658 3. Clustering resolution: Cluster proportions were calculated for the higher-resolution Pheno-
 659 Graph clusters instead of metaclusters. A new interaction prior was constructed based on
 660 cluster-level R-L expression. A new DIISCO model was trained using the cluster-level pro-
 661 portions and interaction prior.
- 662 4. Clustering method: Same as **3**, but cluster proportions were calculated for Leiden clusters
 663 instead of PhenoGraph clusters, as described in Section CAR-T Data Preprocessing - Leiden
 664 comparison.

665 R-L Comparison

666 CellPhoneDB version 2.0.0 was applied to generate interactions in experiment C. To filter predicted
 667 interactions, we only reported receptor-ligand pairs that had non-zero counts in the respective sender

668 and receiver clusters and $p < 0.05$. For running CellChat in RStudio, we used the default human
669 CellChat database ([R Core Team, 2022](#); [Jin et al., 2021](#)). For both methods, all time points were
670 aggregated to increase statistical power. To compare results between all 3 methods, we focused on
671 the MEC→Exhausted interaction. Spearman’s and Pearson’s correlations were calculated with the
672 `SciPy` package, and mutual information was calculated using `sklearn` package for the union of all
673 R-L pairs predicted by any of the three methods.

674 We further ran CellphoneDB on ‘early’ and ‘late’ time points grouped together. ‘Early’ was
675 defined as the first 5 time points and ‘late’ was defined as the last 4 time points. We then ran
676 cellphoneDB and processed the predicted interactions as mentioned above. To compare to DIISCO,
677 we limited predicted interactions to ones that were in either the ‘early’ or ‘late’ set, not both. We
678 then compared the predicted R-L pairs from DIISCO and from these 2 bucketed groups, identifying
679 R-L pairs shared between both methods and ones unique to either method.

680 **Data Access**

681 The DIISCO package and notebooks for generating the figures in this manuscript are publicly acces-
682 sible at GitHub (https://github.com/azizilab/DIISCO_public) and as Supplemental Code. All
683 raw and processed sequencing data generated in this study have been submitted to the NCBI
684 Gene Expression Omnibus (GEO; <https://www.ncbi.nlm.nih.gov/geo/>) under accession number
685 GSE255888.

686 **Conflict of Interest**

687 C.J.W. is an equity holder of BioNTech and receives research funding from Pharmacyclics.

688 **Acknowledgements**

689 We are thankful to David Blei and Dana Pe’er for helpful feedback and discussions. We are also
690 thankful to Gitte Aasbjerg for help and guidance in demultiplexing the CAR-T data. This work was
691 made possible by support from the National Institute of Health (NIH) NCI grants R00CA230195,
692 P01CA229092, Leukemia & Lymphoma Society grant SCOR-22937-22, and the MacMillan Family
693 and the MacMillan Center for the Study of the Non-Coding Cancer Genome at the New York

694 Genome Center. C.P. was supported by the Columbia University Kaganov Fellowship. K.M. was
695 supported by the Richard K. Lubin Family Foundation Fellowship.

696 Contributions

697 C.Y.P, S.M, E.A conceived and supervised the study. C.Y.P, S.M, N.B, E.A designed and devel-
698 oped DIISCO. N.B designed pyro implementation of DIISCO. C.Y.P, S.M, N.B, K.M, E.A, C.J.W
699 analyzed and interpreted results. S.G, S.L, T.H designed and performed all *in vitro* experiments
700 and sequencing. D.A.K, K.J.L, C.J.W, and E.A offered project guidance and troubleshooting.

701 References

702 Aitchison J. 2003. *The statistical analysis of Compositional Data*. Blackburn Press.

703 Azizi E, Carr AJ, Plitas G, Cornish AE, Konopacki C, Prabhakaran S, Nainys J, Wu K, Kiseliovas
704 V, Setty M, et al.. 2018. Single-cell map of diverse immune phenotypes in the breast tumor
705 microenvironment. *Cell* **174**: 1293–1308.

706 Bachireddy P, Azizi E, Burdziak C, Nguyen VN, Ennis CS, Maurer K, Park CY, Choo ZN, Li S,
707 Gohil SH, et al.. 2021. Mapping the evolution of t cell states during response and resistance to
708 adoptive cellular therapy. *Cell reports* **37**.

709 Bingham E, Chen JP, Jankowiak M, Obermeyer F, Pradhan N, Karaletsos T, Singh R, Szerlip
710 P, Horsfall P, and Goodman ND. 2019. Pyro: Deep universal probabilistic programming. *The*
711 *Journal of Machine Learning Research* **20**: 973–978.

712 Blei DM, Kucukelbir A, and McAuliffe JD. 2017. Variational inference: A review for statisticians.
713 *Journal of the American statistical Association* **112**: 859–877.

714 Browaeys R, Saelens W, and Saeys Y. 2020. Nichenet: modeling intercellular communication by
715 linking ligands to target genes. *Nature methods* **17**: 159–162.

716 Bui TM, Wiesolek HL, and Sumagin R. 2020. Icam-1: A master regulator of cellular responses in
717 inflammation, injury resolution, and tumorigenesis. *Journal of Leucocyte Biology* **108**: 787–799.

- 718 Delabie J, Ceuppens J, Vandenberghe P, de Boer M, Coorevits L, and De Wolf-Peeters C. 1993.
719 The b7/bb1 antigen is expressed by reed-sternberg cells of hodgkin’s disease and contributes to
720 the stimulating capacity of hodgkin’s disease-derived cell lines. *Blood* **82**: 2845–2852.
- 721 Dorfman D, Schultze J, Shahsafaei A, Michalak S, Gribben J, Freeman G, Pinkus G, and Nadler
722 L. 1997. In vivo expression of b7-1 and b7-2 by follicular lymphoma cells can prevent induction
723 of t-cell anergy but is insufficient to induce significant t-cell proliferation. *Blood* **90**: 4297–4306.
- 724 Dürr C, Hanna B, Schulz A, Lucas F, Zucknick M, Benner A, Clear A, Ohl S, Öztürk S, Zenz T,
725 et al.. 2018. Tumor necrosis factor receptor signaling is a driver of chronic lymphocytic leukemia
726 that can be therapeutically targeted by the flavonoid wogonin. *Haematologica* **103**: 688–697.
- 727 Efremova M, Vento-Tormo M, Teichmann SA, and Vento-Tormo R. 2020. Cellphonedb: inferring
728 cell–cell communication from combined expression of multi-subunit ligand–receptor complexes.
729 *Nature protocols* **15**: 1484–1506.
- 730 He Y, Vlaming M, van Meerten T, and Bremer E. 2022. The implementation of tnfrsf co-stimulatory
731 domains in car-t cells for optimal functional activity. *Cancers* **14**: 299.
- 732 Jin S, Guerrero-Juarez CF, Zhang L, Chang I, Ramos R, Kuan CH, Myung P, Plikus MV, and Nie
733 Q. 2021. Inference and analysis of cell-cell communication using cellchat. *Nature communications*
734 **12**: 1088.
- 735 Kingma DP and Ba J. 2014. Adam: A method for stochastic optimization. *arXiv preprint*
736 *arXiv:1412.6980* .
- 737 Kingma DP and Welling M. 2022. Auto-encoding variational bayes.
- 738 Kumar MP, Du J, Lagoudas G, Jiao Y, Sawyer A, Drummond DC, Lauffenburger DA, and Raue
739 A. 2018. Analysis of single-cell rna-seq identifies cell-cell communication associated with tumor
740 characteristics. *Cell reports* **25**: 1458–1468.
- 741 Levine J, Simonds E, Bendall S, Davis K, El-ad D, Tadmor M, Litvin O, Fienberg H, Jager A,
742 Zunder E, et al.. 2015. Data-driven phenotypic dissection of aml reveals progenitor-like cells that
743 correlate with prognosis. *Cell* **162**: 184–197.

- 744 Li J, Hubisz MJ, Earlie EM, Duran MA, Hong C, Varela AA, Lettera E, Deyell M, Tavora B, Havel
745 JJ, et al.. 2023. Non-cell-autonomous cancer progression from chromosomal instability. *Nature*
746 pp. 1–9.
- 747 Li S, Xing W, Kirby M, and Zhe S. 2020. Scalable variational gaussian process regression networks.
748 *arXiv preprint arXiv:2003.11489* .
- 749 Lönnberg T, Svensson V, James KR, Fernandez-Ruiz D, Sebina I, Montandon R, Soon MS, Fogg
750 LG, Nair AS, Liligeto UN, et al.. 2017. Single-cell rna-seq and computational analysis using
751 temporal mixture modeling resolves th1/tfh fate bifurcation in malaria. *Science immunology* **2**:
752 eaal2192.
- 753 Maurer K, Park C, Mani S, Borji M, Penter L, Jin Y, Zhang JY, Shin C, Brenner JR, Southard J,
754 et al.. 2024. Coordinated immune cell networks in the bone marrow microenvironment define the
755 graft versus leukemia response with adoptive cellular therapy. *bioRxiv* .
- 756 Molica S, Dattilo A, Mannella A, Levato D, and Levato L. 1995. Expression on leukemic cells and
757 serum circulating levels of intercellular adhesion molecule-1 (icam-1) in b-cell chronic lymphocytic
758 leukemia: implications for prognosis. *Leukemia research* **19**: 573–580.
- 759 Musolino C, Alonci A, Allegra A, Bellomo G, Spatari G, Pernice F, Squadrito G, Quartarone C,
760 Tringali O, and Quartarone M. 1996. Circulating levels of intercellular adhesion molecule-1 (icam-
761 1) and soluble interleukin 2 receptors (il-2r) in patients with b cell chronic lymphocytic leukaemia.
762 *Rivista Europea per le Scienze Mediche e Farmacologiche= European Review for Medical and*
763 *Pharmacological Sciences= Revue Europeenne Pour les Sciences Medicales et Pharmacologiques*
764 **18**: 113–118.
- 765 Nicholson I, Lenton K, Little D, Decorso T, Lee F, Scott A, Zola H, and Hohmann A. 1997. Construc-
766 tion and characterisation of a functional cd19 specific single chain fv fragment for immunotherapy
767 of b lineage leukaemia and lymphoma. *Molecular Immunology* **34**: 1157–1165.
- 768 R Core Team. 2022. *R: A Language and Environment for Statistical Computing*. R Foundation for
769 Statistical Computing, Vienna, Austria.
- 770 Rasmussen CE and I WCK. 2008. *Gaussian processes for machine learning*. MIT Press.

- 771 Sievers C, Craveiro M, Friedman J, Robbins Y, Yang X, Bai K, Nguyen A, Redman JM, Chari
772 R, Soon-Shiong P, et al.. 2023. Phenotypic plasticity and reduced tissue retention of exhausted
773 tumor-infiltrating t cells following neoadjuvant immunotherapy in head and neck cancer. *Cancer*
774 *Cell* **41**: 887–902.
- 775 Stacchini A, Aragno M, Vallario A, Alfarano A, Circosta P, Gottardi D, Faldella A, Rege-Cambrin
776 G, Thunberg U, Nilsson K, et al.. 1999. Mec1 and mec2: two new cell lines derived from b-chronic
777 lymphocytic leukaemia in polymphocytoid transformation. *Leukemia research* **23**: 127–136.
- 778 Tirosh I, Izar B, Prakadan SM, Wadsworth MH, Treacy D, Trombetta JJ, Rotem A, Rodman C,
779 Lian C, Murphy G, et al.. 2016. Dissecting the multicellular ecosystem of metastatic melanoma
780 by single-cell rna-seq. *Science* **352**: 189–196.
- 781 Türei D, Korcsmáros T, and Saez-Rodriguez J. 2016. Omnipath: guidelines and gateway for
782 literature-curated signaling pathway resources. *Nature Methods* **13**: 966–967.
- 783 Vyth-Dreese F, Boot H, Dellemijn T, Majoor D, Oomen L, Laman J, Van Meurs M, De Weger
784 R, and De Jong D. 1998. Localization in situ of costimulatory molecules and cytokines in b-cell
785 non-hodgkin’s lymphoma. *Immunology* **94**: 580–586.
- 786 Wilk AJ, Rustagi A, Zhao NQ, Roque J, Martínez-Colón GJ, McKechnie JL, Ivison GT, Ranganath
787 T, Vergara R, Hollis T, et al.. 2020. A single-cell atlas of the peripheral immune response in
788 patients with severe covid-19. *Nature medicine* **26**: 1070–1076.
- 789 Wilson AG, Knowles DA, and Ghahramani Z. 2011. Gaussian process regression networks. *arXiv*
790 *preprint arXiv:1110.4411* .
- 791 Wolf FA, Angerer P, and Theis FJ. 2018. Scanpy: large-scale single-cell gene expression data
792 analysis. *Genome biology* **19**: 1–5.
- 793 Yofe I, Dahan R, and Amit I. 2020. Single-cell genomic approaches for developing the next generation
794 of immunotherapies. *Nature medicine* **26**: 171–177.

795 Figure Captions

796 **Figure 1: Overview of DIISCO framework.** (A) General workflow of the DIISCO algorithm
 797 including inputs and outputs. Cell type proportions are computed from scRNA-seq data in each
 798 time-point. Expression of R-L complexes is incorporated to obtain time-resolved interactions be-
 799 tween cell types. (B) Network diagram of model framework. (C) Graphical model of DIISCO,
 800 including all hyperparameters. Latent variables are depicted as white circles, and observed vari-
 801 ables are depicted as yellow-shaded circles. (D) Process for incorporating domain knowledge on
 802 R-L interactions as a prior for cell-cell interactions into DIISCO.

803

804 **Figure 2: Simulated data and results.** (A) Simulated data for 5 cell types generated using
 805 the process described in section 3.1 with noise parameter set to 0.1 and 40 sampled timepoints.
 806 Non-uniform sampling of timepoints increases complexity. Dots represent datapoints for each of
 807 the 5 cell types. Orange line is the average learned DIISCO dynamics after fitting the data over
 808 1000 samplings. Shaded region shows 95% confidence intervals. No normalization was used. (B)
 809 Interactions inferred by DIISCO between the cell types shown in (a). Ground truth W interactions
 810 are shown in dotted lines while DIISCO predictions are solid lines. Only dynamic interactions with
 811 $W(t) > 0.1$ in at least one time point t for either true W or learned W are shown. (C) Same as in
 812 A, except noise parameter set to 0.5. (D) Same as in B except learned interactions for the noisier
 813 dataset shown in (C). (E) Method robustness to number of timepoints: R^2 calculated between
 814 inferred and ground-truth $W(t)$. Mean and SD across 5 iterations are shown. (F) Runtime for
 815 varying number of clusters and timepoints. (G) Table demonstrating DIISCO performance com-
 816 pared to Linear Model (LM) and Rolling Linear Model (RLM) as described in **Methods** for 40
 817 timepoints. Metrics for different numbers of time points from 10-90 can be found in Supplementary
 818 Tables 1 and 2. Each model was tested over 10 iterations and mean and standard deviation are
 819 shown for each metric across all iterations. Model acronyms denote the following: LM-PRIOR =
 820 Linear Model with prior. LM = Linear Model. RLM-PRIOR = Rolling Linear Model with prior.
 821 RLM = Rolling Linear Model. Model details can be found in **Methods**. Comparison metrics used
 822 are as follows: R^2_Y , R^2_W : R^2 value comparing predictions to ground truth for dynamics (Y) or
 823 interactions (W). Higher is better. $RMSE_Y$, $RMSE_W$: Root mean squared error for dynamics

824 (Y) or interactions (W). Lower is better. AUC: Area under ROC curve. Higher is better. AUPRC:
 825 Area under Precision-Recall curve. Higher is better. F1: Max F1 score. Higher is better. AUC,
 826 AUPRC, and F1 scores calculated comparing predicted interactions to ground truth interactions.

827

828 **Figure 3: CAR-T experimental setup and data preprocessing.** (A). Overview of data
 829 collection process and analysis of co-culture experiments outlined in **Supplementary Table 1**).
 830 (B-D) 2D UMAP projection of 9082 single-cell transcriptomes from Experiment C colored by time
 831 point (B), cluster and cell type assignment (C), and average expression of different gene set markers
 832 (D) used to define metaclusters. (E) Heatmap of average cluster expression of individual genes
 833 used in gene set analysis, Z -scored across all clusters. (F) Prior constructed for DIISCO input,
 834 generated as explained in **Methods**.

835

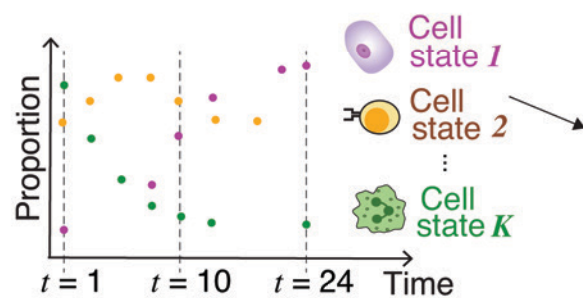
836 **Figure 4: DIISCO performance on CAR-T Experiment C.** (A) Temporal dynamics
 837 of cell types. Data points represent the measured proportion of cell types over time, and DIISCO
 838 output is shown as inferred mean (solid line) and 85% confidence intervals (shaded area) of y for
 839 each cell type. Additional experiments are shown in **Supplementary Fig. 2**. (B-C) Inferred W
 840 interaction matrix at two example time points (B) and over the entire co-culture time window (C).
 841 Network node size reflects cell type proportion at that timepoint; arrows and their width designate
 842 the direction and strength of inferred interactions respectively. (D) Average interaction strength
 843 between clusters as a function of varying prior thresholds. The threshold indicates the minimum
 844 number of R-L interactions between two cluster pairs needed to denote a 1 in the prior matrix.
 845 (E) Rank of average interaction strengths as a function of varying prior thresholds. (F) Average
 846 interaction score with downsampling total cell number. (G-H) W interaction over time between
 847 Exhausted T cell and MEC1 cells (G) and Exhausted-Activated T cells (H) for different percentages
 848 of dropped cells.

849

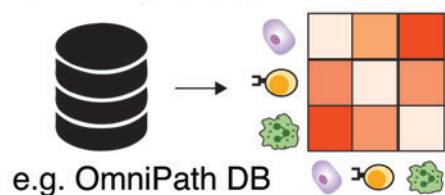
850 **Figure 5: Comparing predicted R-L pairs with existing methods** (A) R-L pairs highly
 851 correlated with DIISCO predicted $W_{Exhausted \leftrightarrow MEC}$ interaction. Expression of ligands are shown
 852 in blue, receptors in orange (left axis), and interaction strength in red (right axis). (B) Comparison
 853 of DIISCO predicted R-L pairs with those predicted using Cellchat (CC) or CellphoneDB (CDB).

854 Correlations between paired R-Ls shown for the $W_{MEC \rightarrow ExhaustedTcell}$ link. p-values calculated with
855 MWU test. (C) Evaluating temporal correlation of predicted RLs using each method: DIISCO,
856 CellphoneDB (CDB) and Cellchat (CC). A + B refer to RL pairs predicted by method A and B.
857 Table shows 3 different metrics calculated for all R-L pairs: Pearson's correlation, mutual informa-
858 tion (MI), and Spearman's correlation. Mean values +/- SD are quantified, with the top 3 highest
859 scores in **bold** and the highest score underlined.

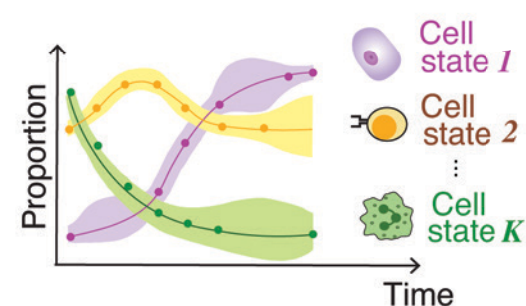
A Input 1: cell type proportions over time



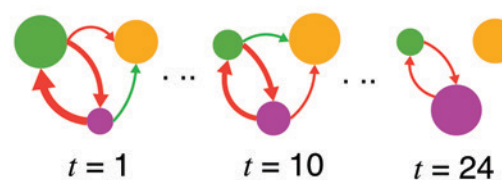
Input 2: incorporate prior knowledge from R-L database



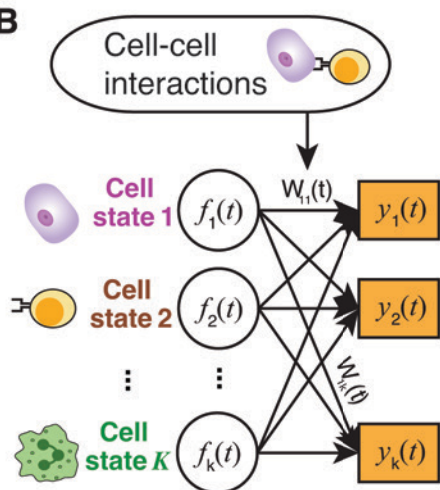
Output 1: predicted cell type proportions



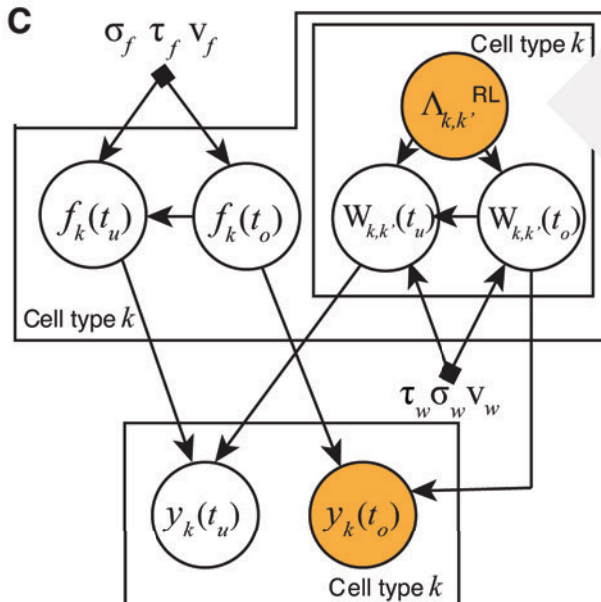
Output 2: inferred dynamic cell-cell interactions



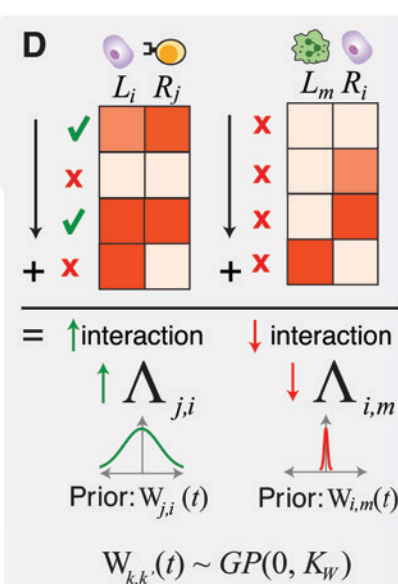
B

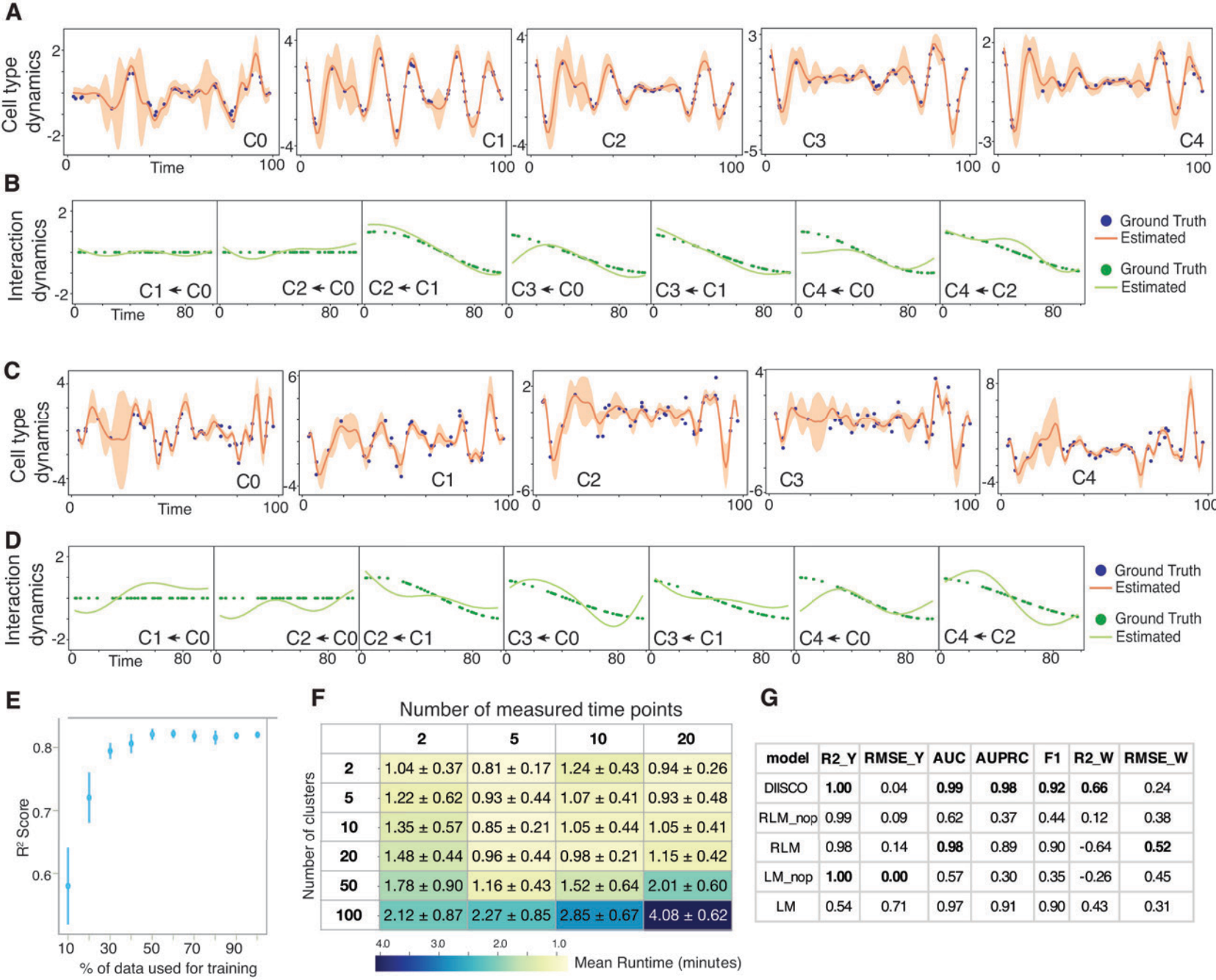


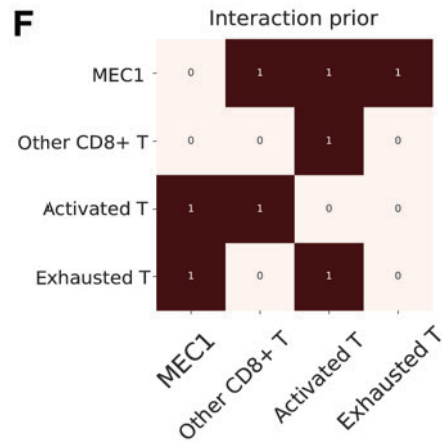
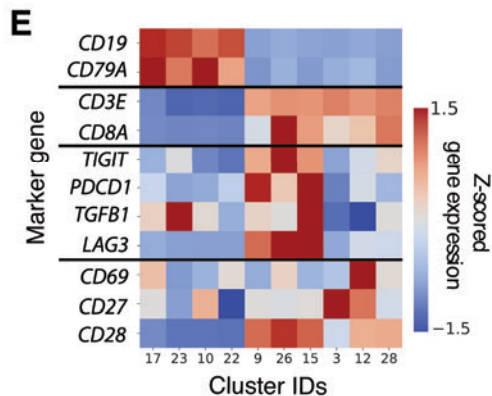
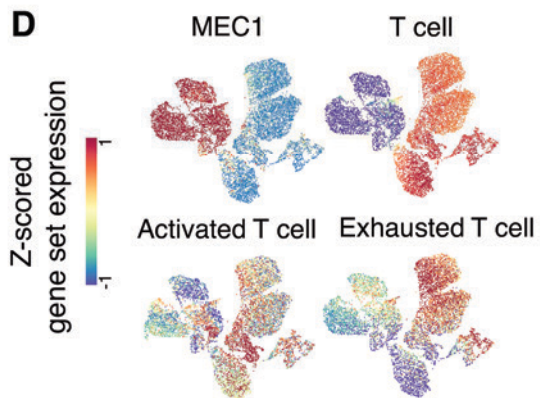
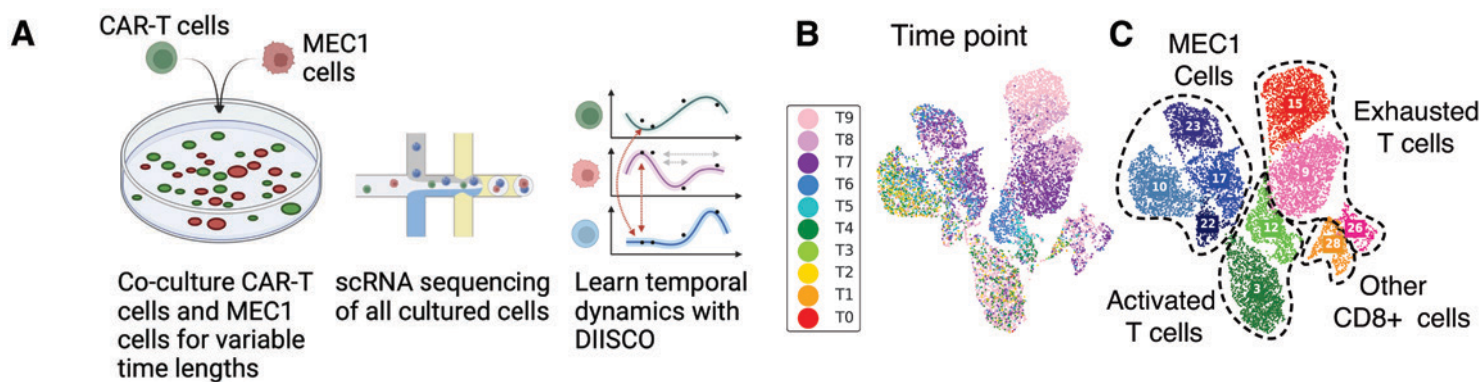
C

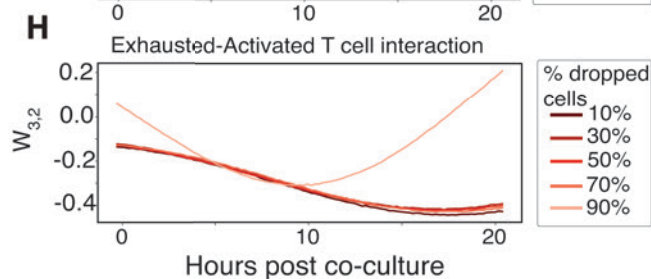
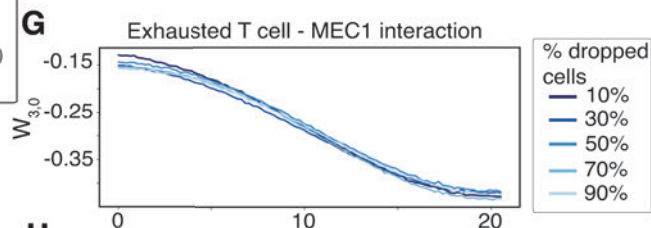
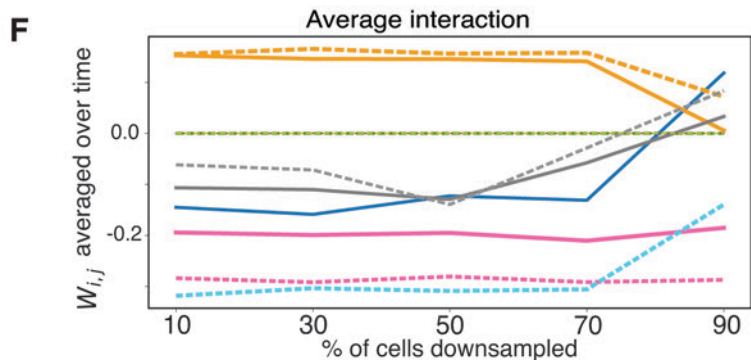
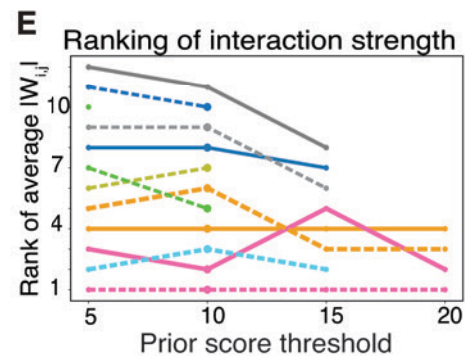
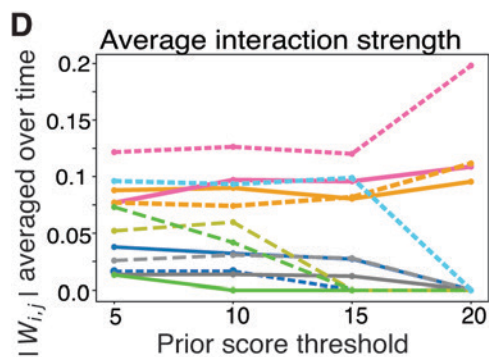
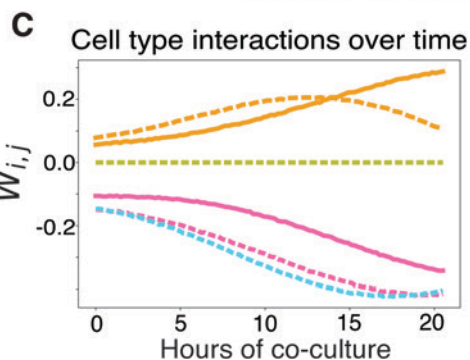
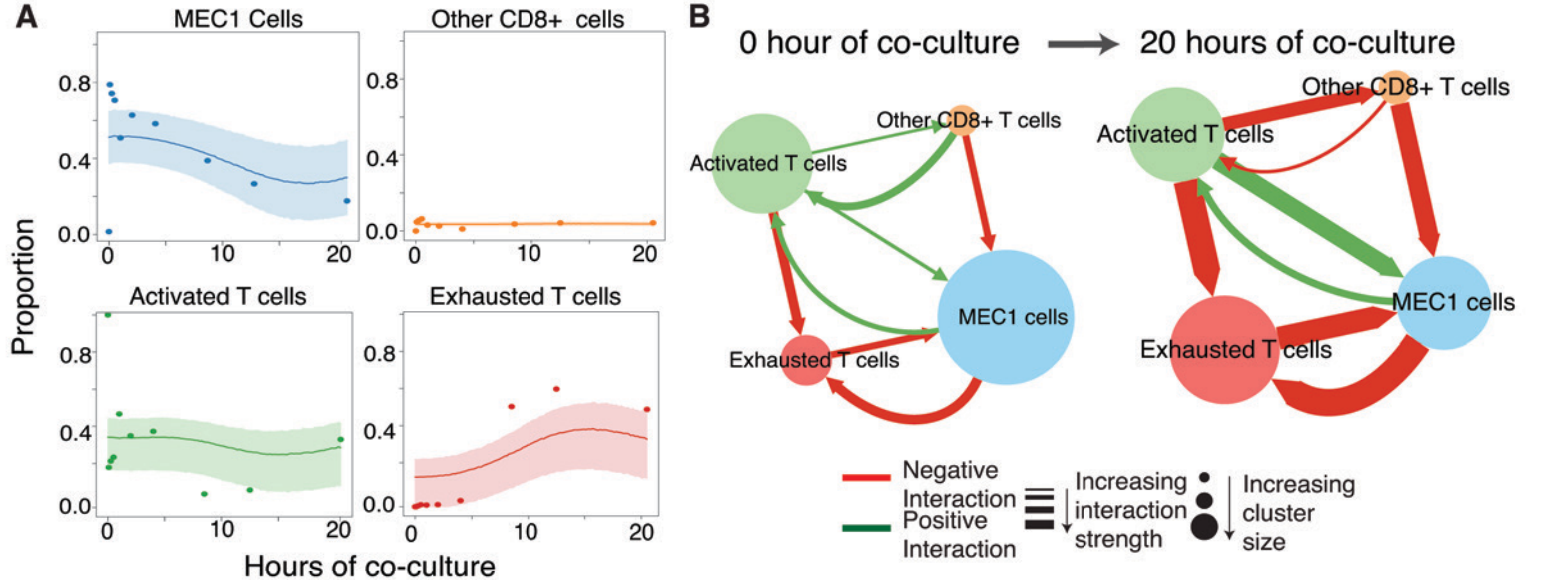


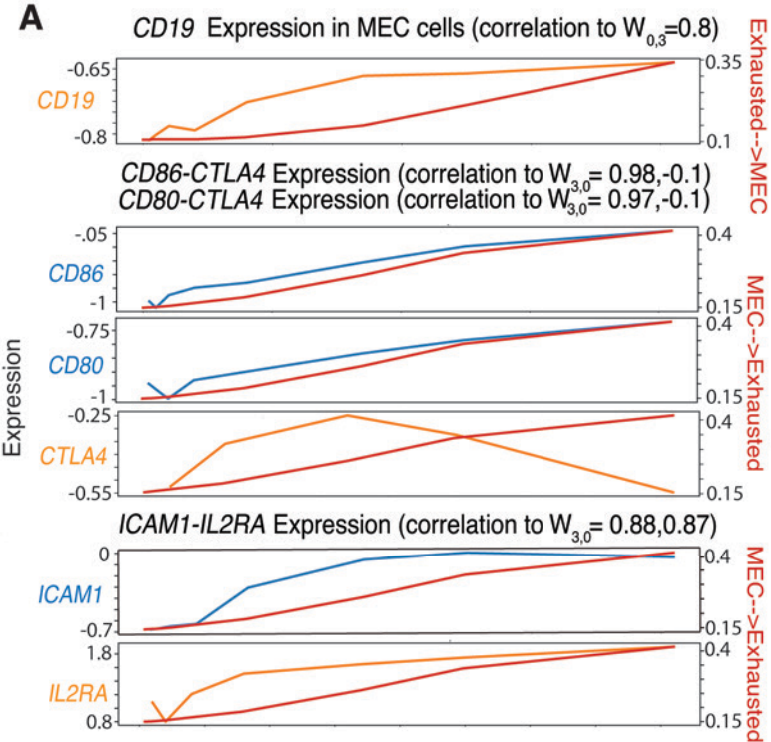
D



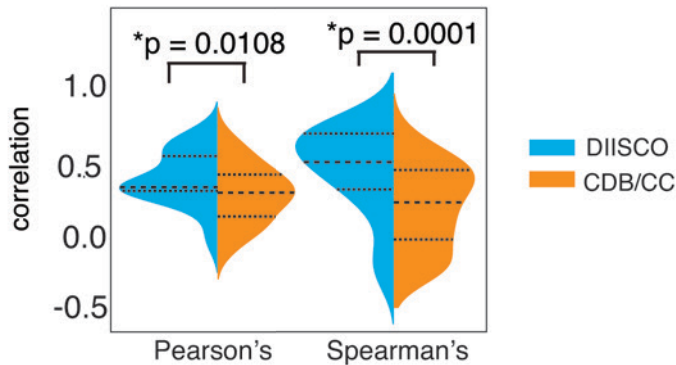








B Correlations of predicted R-Ls (MEC1-->Exhausted T cell)



C

	Pearson's \pm std	MI \pm std	Spearman's \pm std
CC	0.356 \pm 0.133	0.186 \pm 0.099	0.042 \pm 0.333
CC + CDB	0.136 \pm 0.173	0.067 \pm 0.09	0.125 \pm 0.114
CDB	0.345 \pm 0.232	0.112 \pm 0.112	0.339 \pm 0.253
DIISCO	0.462 \pm 0.197	0.083 \pm 0.114	0.39 \pm 0.317
DIISCO + CC	0.381 \pm 0.186	0.252 \pm 0.082	0.641 \pm 0.303
DIISCO + CDB	0.569 \pm 0.201	0.073 \pm 0.084	0.482 \pm 0.265