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## Research

# Low-pass sequencing increases the power of GWAS and decreases measurement error of polygenic risk scores compared to genotyping arrays

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Low-pass sequencing (sequencing a genome to an average depth less than 1× coverage) combined with genotype imputation has been proposed as an alternative to genotyping arrays for trait mapping and calculation of polygenic scores. To empirically assess the relative performance of these technologies for different applications, we performed low-pass sequencing (targeting coverage levels of 0.5× and 1×) and array genotyping (using the Illumina Global Screening Array [GSA]) on 120 DNA samples derived from African- and European-ancestry individuals that are part of the 1000 Genomes Project. We then imputed both the sequencing data and the genotyping array data to the 1000 Genomes Phase 3 haplotype reference panel using a leave-one-out design. We evaluated overall imputation accuracy from these different assays as well as overall power for GWAS from imputed data and computed polygenic risk scores for coronary artery disease and breast cancer using previously derived weights. We conclude that low-pass sequencing plus imputation, in addition to providing a substantial increase in statistical power for genome-wide association studies, provides increased accuracy for polygenic risk prediction at effective coverages of ~0.5× and higher compared to the Illumina GSA.

[Supplemental material is available for this article.]

Thousands of variants on the human genome associated with hundreds of complex traits and diseases have been reproducibly and robustly identified since the first large genome-wide association studies (GWASs) for complex disease were performed in the early years of this century (The Wellcome Trust Case Control Consortium 2007; Yang et al. 2010; Visscher et al. 2012; Sella and Barton 2019). Results from these studies have had an enormous impact on the understanding of the genetic architecture underlying complex traits in humans, with these studies playing an essential part in bringing the current understanding full circle back to Fisher's original infinitesimal model compared to the gene-centric model focused upon in the preceding decades (Judson 1979; Risch et al. 1999; Walsh and Lynch 2018).

The ability to systematically dissect the genetic architecture of complex traits influenced by hundreds or thousands of genetic variants has largely been enabled by the dense genotyping array, which cost-effectively assays the genome of an individual at hundreds of thousands to millions of loci (Visscher et al. 2012). Imputation of the resulting genotypes to existing haplotype reference panels further allows evaluation of genetic variants which are not directly assayed, often resulting in total callsets many times the number of directly assayed loci, and is now standard practice in preparing genomic data sets for GWAS (Li et al. 2009; Marchini and Howie 2010).

As genome sequencing costs have decreased over the past decade, sequencing-based alternatives to genotyping arrays have been the subject of growing interest (Wetterstrand 2019). Specifically, low-coverage shotgun whole-genome sequencing followed by imputation has been utilized for a number of problems in statistical and population genetics, from providing the backbone for graph-based pangenomes in sorghum to trait mapping in human phar-

macogenetics (Cai et al. 2015a; Liu et al. 2018; Gilly et al. 2019; Homburger et al. 2019; Wasik et al. 2019; Jensen et al. 2020; Tran et al. 2020; Rubinacci et al. 2021). As an intuition for why this approach is useful, a sample sequenced at a target coverage of 0.5× is expected to have at least one read on 33 million of the 85 million sites in the 1000 Genomes Phase 3 release, whereas a genotyping array will probe a number of variants which is one to two orders of magnitude fewer, albeit with higher average accuracy (The 1000 Genomes Project Consortium 2015).

For many use cases, there are a number of advantages to low-pass sequencing (lps) over genotyping arrays; for example, (1) there is a lack of ascertainment bias with regard to which variants/sites on the genome are assayed, (2) sequence data can be used to discover novel variation both at the sample or population level (such as in Tran et al. 2020; Liu et al. 2018), (3) massively parallel low-pass sequencing can be achieved by multiplexing large numbers of samples to reduce cost, and (4) the fact that the average expected accuracy of a sample's imputed genotypes can be fine-tuned by adjusting the target coverage for the sample, something which is useful when designing experiments within real-world logistical or budgeting constraints (see Pasaniuc et al. 2012 for a detailed simulation-based cost-benefit analysis of low-pass sequencing compared to genotyping arrays for GWAS study designs).

However, studies in the literature which investigate the applications of low-pass sequencing often do so by means of simulation or by down-sampling (often already-aligned) sequence reads from samples previously sequenced at higher coverages (Gilly et al. 2019; Homburger et al. 2019). Although useful, these approaches

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**Table 1.** Details of experiments conducted; experiments A–D were based on low-pass sequencing (lpSeq) whereas experiment E used the Illumina GSA v3.0

Experiment	Mean coverage	Samples	Assay	Library prep	Sequencer
A	0.67	120 (3 replicates)	lpSeq	KAPA HyperPlus	Illumina HiSeq X
B	1.25	120 (3 replicates)	lpSeq	KAPA HyperPlus	Illumina HiSeq X
C	1.20	1 (30 replicates)	lpSeq	KAPA HyperPlus	Illumina HiSeq X
D	1.26	60 (1 replicate)	lpSeq	MGI Easy	BGISeq 500
E (array)	NA	120 (3 replicates)	Illumina GSA v3.0	NA	NA

are unable to capture the real-world idiosyncrasies of data generation in extremely low coverage sequencing and ignore factors such as the use of different library preparation methods which are optimized for sequencing at given target coverages (Aird et al. 2011; Jones et al. 2015).

Here, in order to more realistically represent real-world results, we perform an investigation of low-pass sequencing data where the low-coverage genomes are obtained not by down-sampling higher-coverage samples but by direct sequencing to extremely low target coverages (0.5× and 1.0×). As a point of comparison, we chose to assay the same samples on the Illumina Global Screening Array (GSA), a modern genotyping array specifically designed to capture multi-ethnic genetic variation. We chose these coverages because the all-in cost of library preparation, sequencing, and data analysis for a 0.5× target coverage sample was approximately at parity with the Illumina GSA (as of 2019) and that for 1.0× target coverage sequencing was fast approaching the same with historically dropping sequencing costs (Wetterstrand 2019).

## Results

### Experimental overview

In order to compare the relative performance of low-pass sequencing and genotyping arrays across populations, we selected 60 EUR and 60 AFR individuals (Supplemental Table 1) from the 1000 Genomes Phase 3 release (1KGP3) (The 1000 Genomes Project Consortium 2015) on which to perform five experiments (Table 1; Supplemental Table 2), which we denote experiments A–E.

The samples column describes the number of unique cell lines and the number of replicates run for each of them. Library prep was performed by Gencove for experiments A–C, and libraries were sequenced on the Illumina HiSeq X. For experiment D, DNA was sent to BGI Americas for library prep and sequencing. Empirical coverage for each sample was calculated by dividing the number of bases sequenced by the size of the human genome (~3.3 Gb).

For experiment A, we performed library prep on and sequenced these 120 unique individuals in triplicate to a target coverage of 0.5× on an Illumina HiSeq X. For experiment B, we performed library prep on and sequenced these 120 unique individuals in triplicate to a target coverage of 1.0× on an Illumina HiSeq X. For experiment C, we performed library prep on and sequenced NA12878, a CEU female sample, 30 times to a target coverage of 1.0× on an Illumina HiSeq X. For experiment D, we selected a subset of 30 EUR and 30 AFR samples from the set of 120 unique individuals and sent DNA to BGI Americas for sequencing to a target coverage of 1.0× on a BGISeq 500. For experiment E, we assayed these 120 unique individuals in triplicate on the Illumina GSA v3.0 via the Broad Institute.

Experiment C was conducted principally to illustrate the effects of varying empirical coverage on imputation accuracy (with

all else held equal) and to provide insight into the repeatability of low-pass sequencing on biological replicates and empirical variation in sequencing coverage given a fixed target coverage (Supplemental Fig. 1).

For each assayed sample passing QC (Methods; Supplemental Table 3), we imputed the sequence or genotype array data to the 1KGP3 haplotype reference panel in a leave-one-out manner (Methods) and compared the imputed calls against the left-out genotypes from the 1KGP3 reference panel (which we treated as the “gold-standard” or “truth” set). We also computed polygenic risk scores from the imputed dosages for each sample and the gold-standard truth set for breast cancer (BC) and coronary artery disease (CAD) using variant weights from recent state-of-the-art studies (Inouye et al. 2018; Mavaddat et al. 2019).

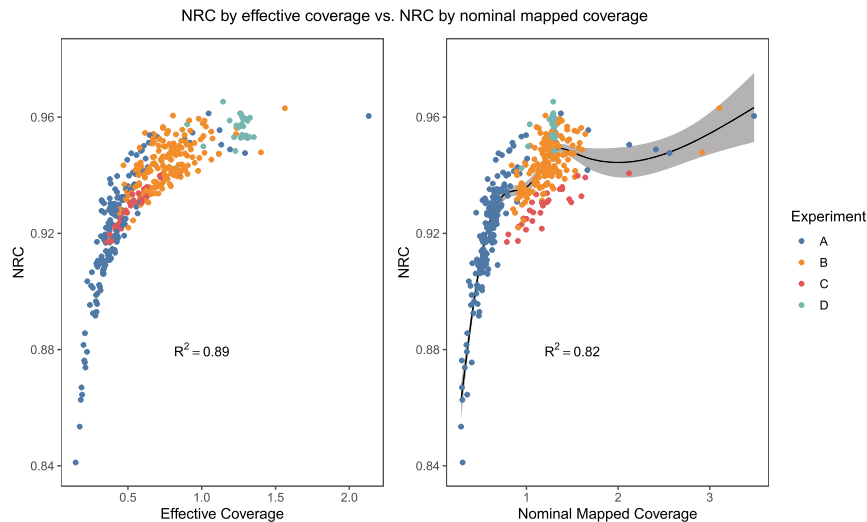
### Defining “effective coverage”

The nominal (mapped) coverage of a sample having undergone whole-genome sequencing is defined as the number of sequenced (and mapped) bases divided by the size of the genome (in this case, ~3.3 Gb). This quantity is useful as an indicator of how much sequence data is available for downstream analysis but does not give any useful information as to how spatially uniform (with respect to the genome coordinate system) the sequenced data are distributed. Spatial uniformity of sequencing reads is particularly important for low-pass sequencing followed by imputation because imputation panels catalog variation across the entire genome, and the imputation quality at a given variant is influenced by the amount of sequence data mapped to regions near that variant and which overlap other variants in the imputation panel.

We therefore introduce the concept of a sequenced sample’s effective coverage  $\lambda_{\text{eff}}$ , which is a function of the fraction of polymorphic sites in a haplotype reference panel covered by at least one sequencing read. Under an idealized Poisson distribution of sequencing reads across sites, this fraction is determined by the sequencing coverage alone (Methods). Specifically, given an imputation panel with  $n$  sites and a set of aligned reads from a single sample, we can compute the fraction of those  $n$  sites covered by at least one read  $f_{\text{covered}}$  and compute that sample’s effective coverage  $\lambda_{\text{eff}} = -\ln(1-f_{\text{covered}})$ .

The advantage of using this quantity rather than nominal coverage as a way to summarize sequence results on a sample, particularly at ultralow coverages, is that the assumptions of an idealized sampling process is “built-in” to its definition. This allows results from, for example, different library preparation methods to be compared on more equal footing (see Fig. 1; Supplemental Figs. 1–3, where experiment D underwent a different library preparation method than experiments A–C).

Indeed, plotting nominal and effective coverage versus non-reference concordance (NRC) (Methods) for all the sequenced samples (Fig. 1) illustrates how NRC is better predicted by a sample’s



**Figure 1.** Nonreference concordance (NRC) (Methods) for imputed SNPs for all EUR samples in experiments A–D plotted against effective coverage  $\lambda_{\text{eff}}$  (left) or nominal mapped coverage (right). We modeled the NRC as the response variable for a  $k = 5$  knot cubic restricted spline with the respective coverage metric as the explanatory variable; the fitted values are shown as a solid line with the surrounding shaded regions representing 95% confidence intervals. The knot locations were set at the 5th, 27.5th, 50th, 72.5th, and 95th percentiles of the respective coverage metrics following Harrell’s rule of thumb (Harrell 2017).

effective coverage rather than the nominal mapped coverage, with cubic restricted spline fits explaining a larger degree of variance when considering effective coverage rather than mapped nominal coverage ( $R^2 = 0.89$  vs.  $R^2 = 0.82$ ). Note that this figure and accompanying fit are not meant to be a rigorous parametric treatment of NRC versus different coverage metrics but are rather meant to provide an intuition.

The results from experiment C illustrate that this pattern also holds across replicates of the same individual, where the only degree of freedom left is the effective coverage of the sample.

Plots of effective coverage versus NRC and overall concordance broken down by variant type (SNPs vs. indels), population, and variant filtration status are shown in Supplemental Figures 4–9 and show qualitatively similar results. When poorly imputed variants are filtered out of a callset (variants with a maximum genotype probability of <90%) (Methods), the relationship between effective coverage and concordance weakens significantly, suggesting that the genotype posterior probabilities generated during imputation are relatively well-calibrated (Methods).

## Comparison of imputation quality metrics across experiments

### Genotype concordance

We then examined how NRC and imputation  $r^2$  varied across experiments A, B, D, and E. In order to do this, for experiments A, B, and E, we took a random sample of one of the replicates run for each unique cell line, such that comparisons across experiments concerned only a single, representative sample of each cell line per experiment (Methods). For experiment D, we retained all samples, as there were no replicates. The remainder of this subsection compares metrics and results from these representative cohorts across experiments. The mean effective coverage of the representative cohorts varied from experiment to experiment (Supplemental Table 4), ranging from an overall (mean  $\pm$  standard

deviation) of  $0.42 \pm 0.22$  for experiment A to  $0.71 \pm 0.17$  for experiment B to  $1.24 \pm 0.11$  for experiment D.

Reference to nonreference and minor allele frequencies are with respect to those found in the 1KGP3. For all analyses, we treated the genotypes in the 1KGP3 for each sample’s cell line as the gold-standard “truth” set.

We observed that imputed genotypes in EUR cohorts were considerably and consistently more accurate than those imputed into the AFR cohorts on average both before and after filtering out poorly imputed variants both for SNPs and indels, with the difference in mean NRC for unfiltered SNPs ranging from 0.0143 in experiment D to 0.08 in experiment E (Table 2). Within each experiment, two-sample unpaired Welch’s  $t$ -tests for differences in means between results for EUR and AFR samples all yielded significant ( $P < 0.001$ ) results.

Furthermore, we observed that genotypes imputed from sequence were consistently and considerably more accurate than those imputed from array data, with the mean AFR NRC being 7% higher for sequence data with an average of 0.4 $\times$  effective coverage compared to the array data (Table 2; Supplemental Tables 5–7). Two-sample paired  $t$ -tests for differences in means between the array results and sequence results in Table 2 (given a superpopulation) all yielded significant ( $P < 0.001$ ) results.

In order to compare performance across the allele frequency spectrum, we computed the mean nonreference concordance for SNPs within a given allele frequency bin within each representative cohort (Fig. 2; Supplemental Fig. 10; Supplemental Table 12). The average NRCs for experiment E’s representative cohorts were significantly lower than those of all other experiments at all frequency bins, and qualitatively similar patterns hold for overall genotype concordance as well (Supplemental Tables 8–11). These results indicate that low-pass sequencing at an effective coverage of  $\sim 0.4\times$  or higher consistently yields more accurate imputed genotype calls at sites of common variation than the Illumina GSA and that this pattern holds across both EUR and AFR cohorts.

In particular, the NRC at low (<5%) allele frequencies in AFR populations often exceeds the corresponding NRC for EUR populations (Supplemental Fig. 11) for the sequence-based experiments. We also observe this pattern for the imputation  $r^2$ s, which we address next.

### Imputation $r^2$

Genotype concordance is an important metric which provides a straightforward and intuitive quantification of the performance of genotype imputation. However, in the context of genome-wide association studies, a more relevant quantity is the imputation  $r^2$ , which is defined as the squared correlation between the imputed dosage and the true genotypes of a given set of samples at a given variant. This is because the imputation  $r^2$  at a given variant is proportional to the expectation of the  $\chi^2$  statistic resulting from an association test at that particular variant, of which the power of the

**Table 2.** Mean and interquartile range (in parentheses) nonreference concordance (NRC) across samples for each representative cohort for unfiltered SNPs by experiment and superpopulation

Superpopulation	Experiment			
	A	B	D	E (array)
AFR	0.9002 (0.8896–0.9089)	0.9217 (0.9123–0.9288)	0.9419 (0.9378–0.9434)	0.8308 (0.8119–0.8425)
EUR	0.9227 (0.913–0.9342)	0.9438 (0.9397–0.9477)	0.9562 (0.9531–0.9594)	0.9067 (0.898–0.9116)

test is a function (Pritchard and Przeworski 2001; Chapman et al. 2003; Marchini 2019). A practical consequence of this is that a proportional increase in the imputation  $r^2$  at a particular variant can be interpreted as the same proportional increase in effective sample size at that variant, so that an increase in mean imputation  $r^2$  across the genome directly corresponds to increased statistical power (Pritchard and Przeworski 2001). This quantity can be computed on a site-by-site basis and stratified into allele frequency bins according to the allele frequencies in the haplotype reference panel.

At common variants (minor allele frequency > 5% in the 1KGP3), the mean imputation  $r^2$  for sequence-based experiments ranged from 0.92 to 0.96 for the EUR representative cohorts compared to a mean  $r^2$  of 0.91 for experiment E, representing an average increase in power of ~1%–6% for samples with mean effective coverages ranging from ~0.47× to 1.24× (Supplemental Tables 4, 15). For the AFR representative cohorts, the mean imputation  $r^2$  for sequence-based experiments ranged from 0.89 to 0.95 compared to 0.83 for the GSA, representing an average increase of power of ~7%–15% for samples with mean effective coverages ranging from ~0.38 to 1.24 (Supplemental Table 15). For all experiments and superpopulations at common variants, the mean dosage  $r^2$  for the imputed sequence was significantly higher ( $P < 0.001$ , two-sample Welch's  $t$ -tests) than the corresponding mean dosage  $r^2$  for the imputed array data.

Stratifying imputation site-wise  $r^2$ s into minor allele frequency bins, we observed that for the sequence-based experiments, the average  $r^2$ s across the allele frequency bins scaled with the average effective coverage of each representative cohort (Fig. 3), in line with the expectation that higher-effective-coverage sequence data affords greater imputation accuracy.

For the AFR cohorts, we observed that sequence-based experiments uniformly outperformed genotyping arrays for all minor allele frequency bins, whereas for EUR cohorts the same was true above minor allele frequencies of 0.01 for all but the cohort with the lowest mean effective coverage, experiment A (Supplemental Fig. 13).

In particular, at minor allele frequencies of ~5% and lower, for a given sequence-based experiment, imputation performance in the AFR cohorts often exceeded performance at similar allele frequencies in the EUR cohorts, a pattern opposite to that which was observed at higher allele frequencies (Supplemental Fig. 13; Supplemental Tables 13, 14). This pattern was not observed for the imputed array data, where the imputation  $r^2$ s for all allele

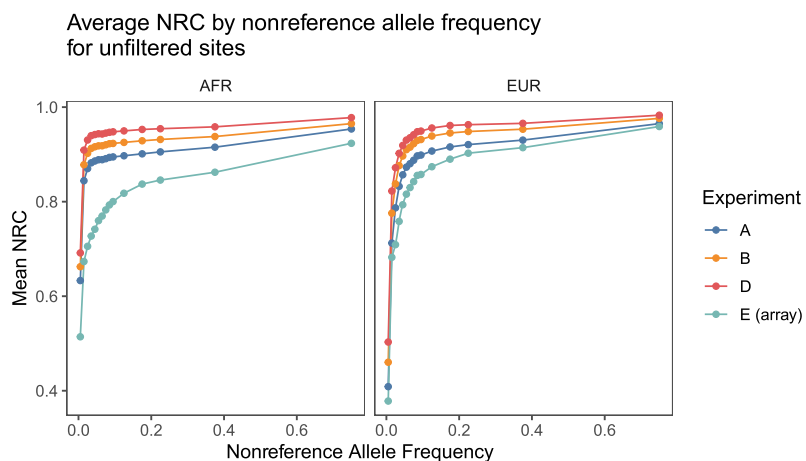
frequency bins were higher in the EUR cohort than in the AFR cohort.

Similarly to Marchini (2019), we hypothesize that this is due to the fact that, at higher allele frequencies, the stronger linkage disequilibrium (LD) structure within European populations dominates and affords more accurate haplotype tagging, whereas at lower allele frequencies, the effects of greater genetic diversity in African populations dominate, resulting in a larger number of possible haplotype combinations and an increased chance that any one rare variant is tagged by at least one of these.

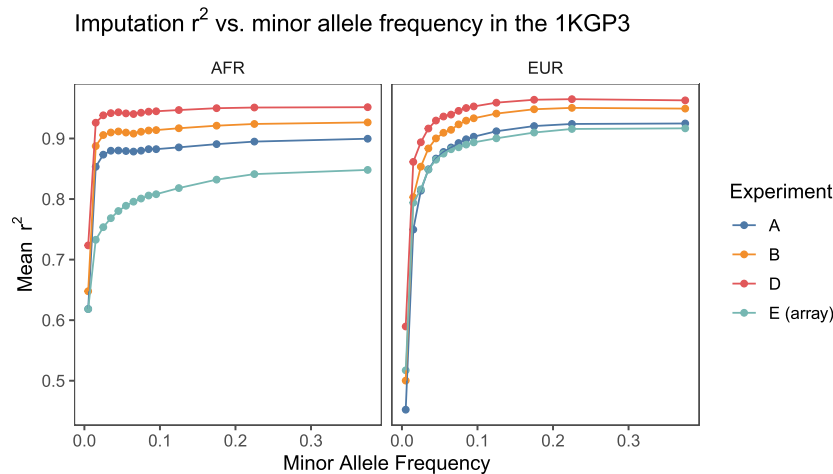
Because low-pass sequencing yields measurements at orders-of-magnitude more sites than genotyping arrays, it is possible to measure a larger range of these possible haplotypes, which is reflected by this pattern holding only for the sequence-based experiments.

### Polygenic risk scores

Polygenic risk scores were calculated from imputed dosages for each sample in all experiments for breast cancer and coronary artery disease using recently published results in order to evaluate the accuracy of PRS estimation across experiments and assay types (Inouye et al. 2018; Mavaddat et al. 2019). We chose to use weights from these studies because of their demonstrated ability to stratify disease risk beyond conventional risk factors. Of the 1,745,179 variants with nonzero effect sizes in the CAD PRS, 1,738,589 (99.6%) were present in the haplotype reference panel, and 225,667 were directly typed on the GSA. Of the 313 variants with nonzero effect sizes in the BC PRS, all were present in the haplotype reference panel, and 75 were directly typed on the GSA.



**Figure 2.** Average nonreference concordance for unfiltered SNPs by superpopulation by nonreference allele frequency in 1KGP3. The NRC for imputed sequence data was consistently higher than the NRC for the imputed GSA data across the allele frequency spectrum. Filtering to confidently imputed variants reveals a similar pattern (Supplemental Fig. 10).



**Figure 3.** Comparison of imputation quality across experiments for each superpopulation. Variants were binned according to their minor allele frequency in the 1KGP3 and imputation  $r^2$  averaged across variants in each bin. For all experiments, the 1KGP3 genotypes were treated as “truth” and imputation  $r^2$  was computed by taking the squared correlation coefficient between the vector of imputed alternate allelic dosages and the truth genotypes. Same results on a log scale are shown in Supplemental Figure 13. Note that imputation performance at low MAF for a given sequencing experiment was often higher in the AFR cohort compared to the EUR cohort.

We compared the PRS estimates from each sample to the “true” PRS calculated for that cell line from the 1KGP3 genotypes (Supplemental Figs. 14, 15). The estimated scores were highly correlated with the true scores for all experiments, and the  $r^2$ s for AFR estimates within experiments and across traits were consistently lower than those for their corresponding EUR counterparts (Supplemental Table 16). This difference was particularly pronounced for the CAD PRS, with  $r^2$ s ranging from 0.96 to 0.99 across experiments for the EUR samples and  $r^2$ s ranging from 0.87 to 0.94 for the AFR samples.

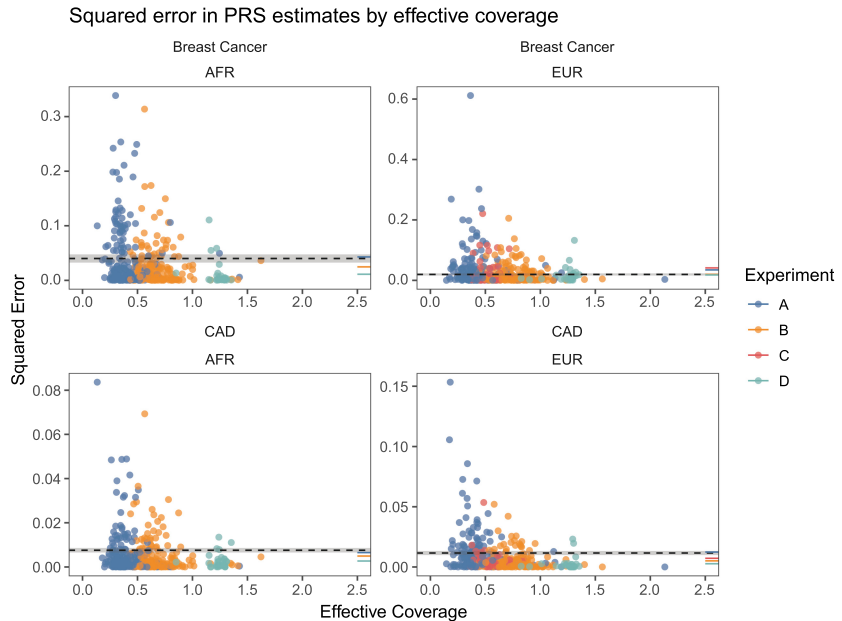
We investigated the relationship between measurement error in PRS (as quantified by the squared error of an estimate) and effective coverage for the sequence-based experiments. Figure 4 shows that the squared error in PRS estimates for all experiments across populations and traits decreases with increasing effective coverage and that the measurement error in samples sequenced to an effective coverage of  $\sim 0.5\times$  or higher generally affords lower measurement error than the array-based estimates, with samples sequenced to an effective coverage of more than  $1\times$  (experiment D) having an approximately three- to fourfold decrease in squared error for both traits in the AFR cohort and the EUR cohort for CAD and approximately the same squared error for the EUR cohort for BC ( $\sim 1.08$ -fold decrease) (Supplemental Tables 17–19). Given a superpopulation and trait, the majority of sequence-based PRS estimates had a

mean squared error that was significantly (at an  $\alpha=0.05$  level) different from the corresponding array-based PRS estimates (Supplemental Table 19).

One thing to note is that the measurement error of PRS estimates depends on the quality of genotypes at the variants involved in computing the PRS, which means that, for arrays, the measurement error will depend on the proportion of the variants involved that are directly typed versus imputed. Here, a minority of the variants comprising the polygenic risk scores (13% and 24% for CAD and BC, respectively) were directly typed on the GSA. Presumably, the measurement error for array-based estimates would be substantially lower in a different situation in which all the variants comprising a PRS are directly typed instead.

## Discussion

The use of dense genotyping arrays followed by imputation to a haplotype reference panel has enabled population-scale genome-



**Figure 4.** For each imputed sample, we computed a PRS for breast cancer and CAD and calculated the squared error of the estimate compared to the PRS of the “truth” genotypes in the 1KGP3. Each dot represents this squared error for each sequenced sample for a given trait and is colored by the experiment to which it belongs. To provide a point of comparison to PRS estimated from imputed array data, we computed the mean squared error for each cell line across array replicates and averaged that across all cell lines. This quantity is represented by the dashed line for each trait and superpopulation along with the standard error of the mean, represented by the shaded regions about each dashed line. The mean squared error for each experiment was calculated in the same way and is rendered as a colored line segment on the *rightmost* margin of each panel. These results indicate that sequencing at effective coverages of 0.5 or higher generally affords lower measurement error in PRS estimates.

wide association studies to become routine in characterizing the genetic architecture of complex traits and disease. An alternative technology is low-pass whole-genome sequencing followed by imputation, which has been successfully used for a number of problems in statistical and population genetics (Pasaniuc et al. 2012; Gilly et al. 2019; Tran et al. 2020) and which was recently shown to recapitulate comparable disease risk stratification performance using a handful of polygenic risk scores derived from imputed array data from an independent cohort (Homburger et al. 2019).

We introduced the notion of effective coverage, a quantity which describes the coverage of a sequenced sample under an ideal sampling process and which is more predictive of imputation accuracy than nominal coverage. We showed that, with increasing effective coverage, genotyping concordance and imputation  $r^2$  increase commensurately, while the measurement error of PRS estimates from the imputed genotypes decreases. We note that because the same amount of sequencing coming from different library preparation methods can yield different effective coverages, systematic comparisons of different library preparation methods on this metric is warranted. For instance, the BGISEQ library prep used in this experiment contrasts to the Illumina prep in that it is a PCR-free workflow, where every replicated copy generated during DNA nanoball rolling-circle replication comes directly from the native genomic fragment (Patterson et al. 2019; Xia et al. 2019). This has the advantage of reducing propagated amplification error and any potential PCR bias of the template due to selective amplification, both of which are well-characterized artifacts of excess PCR.

We observed that, at sites of common variation (MAF > 5%), imputation  $r^2$  was consistently and substantially higher in imputed sequence data compared to imputed array data and in Europeans compared to Africans (Supplemental Table 15). Conversely, at rare variants (MAF < 5%), we observed that imputation  $r^2$  was consistently higher in Africans than Europeans, a result which we hypothesize is due to different aspects of the LD structure in these populations dominating in different regimes of the allele frequency spectrum. A consequence of this observation is that studies of rare variants may (all other things being equal) be more powerful in African-ancestry cohorts as compared to European-ancestry cohorts under some study designs.

We compared PRS estimates for coronary artery disease and breast cancer and found that the measurement error of PRS estimates decreased with increasing effective coverage for sequenced samples. For CAD, we found that low-pass sequence data yielded consistently lower measurement error in PRS estimates in both the African and European cohorts, with samples sequenced to an effective coverage of  $\sim 1.2\times$  yielding an approximately three- to fourfold decrease in mean squared error when compared to PRS estimated from the Illumina GSA. The same decrease was observed for BC estimates in the African cohorts, whereas the mean squared error for BC in the European cohort at that effective coverage was approximately the same as the array estimates ( $\sim 1.08$ -fold relative decrease).

Because imputation accuracy from genotyping array data is known to depend heavily on the size and composition of the haplotype reference panel used (Schurz et al. 2019), it will be interesting to replicate these results for low-pass sequence across different panels, particularly as extremely large panels (e.g., HRC and TOPmed) (McCarthy et al. 2016; Taliun et al. 2021) as well as panels comprising currently underrepresented populations (e.g., NeuroGAP-Psychosis [Stevenson et al. 2019]) come online.

In the context of understanding how genetic variation contributes to phenotypic variance, it has become increasingly clear

in recent years that a whole-genome approach is necessary due to the fact that the degree of polygenicity underlying the majority of complex traits in humans is quite well-approximated by Fisher's infinitesimal model (in which variation arises from infinitely many loci of infinitesimal effect) and, indeed, also that complex traits are mainly driven by noncoding variants (Fisher 1919; Risch et al. 1999; Barton et al. 2017; Boyle et al. 2017). Consequently, methods to accurately assess genetic variation across the whole genome in diverse populations will become increasingly essential to ongoing efforts to elucidate the genetic architecture of complex traits, as well as the population genetic processes which gave rise to it (Berg and Coop 2014; Guo et al. 2018). Our results show that low-pass sequencing is a competitive alternative to genotyping arrays, by affording increased GWAS power and reduced measurement error in the estimation of polygenic risk scores for individuals across multiple populations at a similar price point.

We have discussed the implications of using low-pass sequencing versus genotyping arrays in the context of PRS estimation and GWAS at length, but there are other, orthogonal considerations that should be taken into account when making a choice between lps and genotyping arrays for practical purposes. For instance, sequence data allows more sensitive detection of copy number and structural variation due to the sheer number of reads that are produced even at extremely low coverages (for intuition, 2.2 million 150-bp reads correspond to a coverage of  $0.1\times$  for the human genome) (Dong et al. 2016; Zhou et al. 2018). Analysis of mitochondrial count is also straightforward using sequence data, and having sequence data on the mitochondria enables straightforward DNA contamination detection using read count data (Krause et al. 2010; Cai et al. 2015b). Furthermore, the use of sequencing enables analysis of the microbiome and metagenomic profiling by yielding reads deriving from nonhuman DNA within a given biological sample (Wood et al. 2019).

As low-coverage sequencing becomes increasingly popular as an alternative to genotyping arrays, it is worthwhile to include some discussion on costs and logistical considerations involved in such projects. With sequencing experiments, the two primary factors determining cost are (1) the cost of sequencing, and (2) the cost of sample preparation. For instance, the list price of a NovaSeq S4 flow cell as of October 2020 is  $\approx \$15,000$  US, which corresponds to a sequencing cost of  $(\$15,000/1536) = \$9.76$  per sample for  $0.5\times$  sequencing and  $(\$15,000/768) = \$19.52$  per sample for  $1\times$  sequencing (NovaSeq Reagent Kits; <https://www.illumina.com/products/by-type/sequencing-kits/cluster-gen-sequencing-reagents/novaseq-reagent-kits.html>). On the library preparation side, miniaturized/modified workflows currently allow for library preparation costs of under  $\$10$ /sample (in our specific case, we estimate our costs for the miniaturized Kapa Hyper Prep workflow at around  $\$6$ /sample). The all-in cost of library preparation and sequencing therefore comes out to be just under  $\$16$ /sample for  $0.5\times$  coverage and just under  $\$26$ /sample for  $1\times$  coverage, comparing favorably with the list price of the Illumina GSA (approximately  $\$49$ /sample as of November 2020 [Infinium Global Screening Array 24-pack; <https://www.illumina.com/products/by-type/microarray-kits/infinium-global-screening.html>]).

For future directions, there are methodological advances that could be made in order to fully leverage the information that sequencing provides. Genotyping arrays suffer from ascertainment bias which manifests in two ways: (1) measurements are always made on the same set of loci across the genome; and (2) measurements at a given loci do not allow for novel variant discovery (i.e.,

you have to know what you are looking for) (Nielsen 2004; Lachance and Tishkoff 2013).

Low-pass sequencing by its nature overcomes consideration (1), but whether a problem similar to (2) remains depends on the analytical techniques utilized downstream of actual sequencing. For instance, the current implementation of the imputation tool used here (loimpute [Wasik et al. 2019]) does not allow for variants which are novel to the reference panel to be called, thus causing a similar effect in post-imputation sequence data as consideration (2) in unimputed array data. In other words, this means that the effective upper bound in genotyping accuracy is governed by the composition of the reference panel and whether a particular individual's genetic variation is cataloged therein. A potential methodological improvement would thus be to develop a way to enable novel variant calls at sites with overwhelming read-based evidence.

As research into the genetic architecture of complex disease and traits continues to accelerate, it will become increasingly important for data generation techniques to be as population-agnostic as possible in order to capture global genetic variation in an unbiased manner. Our results demonstrate that low-pass sequencing provides a competitive alternative to genotyping arrays in the context of genome-wide association studies and polygenic risk scoring across diverse populations.

## Methods

### Data generation

Purified genomic DNA (gDNA) from 60 selected individuals of European ancestry and 60 selected individuals of African ancestry from the 1000 Genomes Project Phase 3 was obtained from the NIGMS Human Genetic Cell Repository at the Coriell Institute for Medical Research. Genomic DNA was extracted from immortalized B lymphocytes and eluted in TE buffer (10 mM Tris, pH 8.0/1 mM EDTA) for shipping.

To prepare the 120 gDNA samples for sequencing, 30  $\mu$ L from each was plated and diluted to 10 ng/ $\mu$ L using 10 mM Tris-HCl, and sequencing libraries were prepared in triplicate using a miniaturized version of the KAPA HyperPlus kit (Roche KK8514) with Illumina-compatible KAPA Unique Dual-Indexed Adapters (Roche KK8727).

Following library preparation, a subset volume of 10  $\mu$ L was pooled from each of the resulting libraries. The pooled libraries were purified with a double-sided size-selection using SPRIselect paramagnetic beads (Beckman Coulter Life Sciences B23318) to narrow the library fragment size range and remove dimerized adapters from the samples. To characterize the purified pools, the concentration was measured using the Invitrogen Qubit Fluorometer (Thermo Fisher Scientific Q33238), and the library fragment size was assessed using the Agilent 2100 Bioanalyzer (Agilent G2939BA) with a High Sensitivity DNA Kit (Agilent 5067-4626).

Sequencing of purified library pools of 30 and 60 samples was performed to 0.5 $\times$  coverage and 1 $\times$  target coverages, respectively, using paired-end 150-bp reads on the Illumina HiSeq X platform.

To prepare NA12878 for sequencing 30 times to 1 target coverage, 10  $\mu$ L from the source gDNA sample were aliquoted into 30 separate wells of a 96-well plate and diluted to 10 ng/ $\mu$ L using 10 mM Tris-HCl. Sequencing libraries were prepared from these diluted samples using a miniaturized version of the KAPA HyperPlus kit (Roche KK8514) with Illumina-compatible KAPA Unique Dual-Indexed Adapters (Roche KK8727). The 30 libraries were pooled and purified with a double-sided size-selection using SPRIselect paramagnetic beads (Beckman Coulter Life Sciences B23318),

checked for concentration and fragment size, and sequenced on a single lane of an Illumina HiSeq X flow cell.

A subset of 1  $\mu$ g gDNA from 30 samples selected from each population (60 total) was aliquoted into plates and submitted to BGI Americas Corporation for DNA nanoball library prep and sequencing (DNBseq) using paired-end 100-bp reads on the BGISEQ-500 sequencing instrument.

Sample genotyping was performed using the Infinium Illumina Global Screening Array v3.0 (Illumina 20030770) by the Broad Institute Genomic Services group. Each of the 120 samples was genotyped in triplicate. To prepare the 360 samples for genotyping, a total mass of 1  $\mu$ g gDNA from each sample was aliquoted into barcode-labeled tubes and submitted to the Broad Institute for processing.

### Quality control

Of the 360 samples in experiment A assayed on the Illumina HiSeq X, 351 passed QC and the remainder failed due to contamination or low read count (less than 0.1 $\times$  nominal coverage). Of the 360 samples in experiment B assayed on the Illumina HiSeq X, 350 passed QC and the remainder failed due to contamination or low read count (less than 0.1 $\times$  nominal coverage). Of the 30 samples in experiment B assayed on the Illumina HiSeq X, all 30 passed QC. Of the 60 samples in experiment D sequenced on BGI machines, 58 passed QC and two failed due to contamination. Of the 360 samples in experiment E assayed on the Illumina GSA, 358 passed QC and two failed due to low call rate (below 97%).

See Supplemental Tables 2 and 3 for a more comprehensive breakdown.

### Effective coverage

Consider an idealized sampling process whereby shotgun sequence data is generated for a given sample to a coverage of  $\lambda$ . We can then model the number of reads  $k$  on a site on the genome as a random variable described by a Poisson distribution thus parameterized. Recall that the probability mass function for a Poisson distribution with these parameters is

$$f(k; \lambda) = \frac{\lambda^k e^{-\lambda}}{k!}. \quad (1)$$

Then, the probability that this site is covered by at least one read is

$$P(k > 0; \lambda) = \sum_{k=1}^{\infty} f(k; \lambda) \quad (2)$$

$$= 1 - f(k = 0; \lambda) \quad (3)$$

$$= 1 - e^{-\lambda}. \quad (4)$$

Suppose now that we have a set of  $n$  such sites on the genome (which, in our case, represents the  $n$  sites in a haplotype reference panel) which are all independent and identically distributed. Then, the total number of sites  $X$  covered by at least one read is described by a binomial distribution with  $p = P(k > 0; \lambda) = 1 - e^{-\lambda}$ , which has an expected value of  $E[X] = np = n(1 - e^{-\lambda})$ . Defining  $f_{\text{covered}} = X/n$  as the proportion of sites covered, we have  $E[f_{\text{covered}}] = (1 - e^{-\lambda})$ .

This quantity describes the expected proportion of sites in a haplotype reference panel covered by at least one read under the assumptions described above, and  $f_{\text{covered}}$  is a quantity which can be empirically computed for any given sample that has been sequenced. The definition of effective coverage then follows naturally as that value of  $\lambda$  which one obtains when plugging in an observed  $f_{\text{covered}}$  into the relation

$$\text{Effective coverage} = \lambda_{\text{eff}} := -\ln(1 - f_{\text{covered}}) \quad (5)$$



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